

## 8th Standard- Maths

### Rational Numbers

- Rational numbers on number line**

Rational numbers can be represented on number line in the similar manner like fractions and integers.

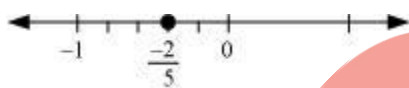
Negative rational numbers are marked to the left of 0 while positive rational numbers are marked to the right of 0.

**Example:** Represent  $-\frac{2}{5}$  on number line.

**Solution:** The given rational number is negative. Therefore, it will lie to the left of 0.

The space between -1 and 0 is divided into 5 equal parts. Therefore, each part represents  $-\frac{1}{5}$ .

Marking  $-\frac{2}{5}$  at 2 units to the left of 0, we obtain the number line as shown below.



- To find rational numbers between any two given rational numbers, firstly we have to make their denominators same and then find the respective rational numbers.

**Example:** Find some rational numbers between  $\frac{1}{6}$  and  $\frac{7}{8}$ .

**Solution:** The L.C.M. of 6 and 8 is 24.

Now, we can write

$$\frac{1}{6} = \frac{1 \times 4}{6 \times 4} = \frac{4}{24}$$

$$\frac{7}{8} = \frac{7 \times 3}{8 \times 3} = \frac{21}{24}$$

Therefore, some of the rational numbers between  $\frac{4}{24} \left( \frac{1}{6} \right)$  and  $\frac{21}{24} \left( \frac{7}{8} \right)$  are

$$\frac{5}{24}, \frac{6}{24}, \frac{7}{24}, \frac{8}{24}, \frac{9}{24}, \frac{10}{24}, \frac{11}{24}, \frac{12}{24}, \frac{13}{24}, \frac{14}{24}, \frac{15}{24}, \frac{16}{24}, \frac{17}{24}, \frac{18}{24}, \frac{19}{24}, \frac{20}{24}$$

- Natural numbers are a collection of all positive numbers starting from 1.
- Whole numbers are a collection of all natural numbers including 0.
- Integers are the set of numbers comprising of all the natural numbers 1, 2, 3 ... and their negatives  $-1, -2, -3 \dots$ , and the number 0.
- Rational numbers are the numbers that can be written in  $\frac{p}{q}$  form, where  $p$  and  $q$  are integers and  $q \neq 0$
- **Closure property**
  - Whole numbers are closed under addition and multiplication. However, they are **not** closed under subtraction and division.
  - Integers are also closed under addition, subtraction and multiplication. However, they are **not** closed under division.
  - Rational numbers:
    1. Rational numbers are closed under addition.  
Example:  $\frac{2}{5} + \frac{3}{2} = \frac{19}{10}$  is a rational number.
    2. Rational numbers are closed under subtraction.  
Example:  $\frac{1}{5} - \frac{3}{4} = \frac{-11}{20}$  is rational number.
    3. Rational numbers are closed under multiplication.  
Example:  $\frac{2}{3} \times \left(\frac{-3}{5}\right) = \frac{-2}{5}$  is a rational number.
    4. Rational numbers are **not** closed under division.  
Example:  $2 \div 0$  is not defined.
- **Commutativity**
  - Whole numbers are commutative under addition and multiplication. However, they are not commutative under subtraction and division.
  - Integers are commutative under addition and multiplication. However, they are not commutative under subtraction and division.
  - Rational numbers:
    1. Rational numbers are commutative under addition.

Example:

$$\frac{2}{3} + \left(\frac{-3}{2}\right) = \left(\frac{-3}{2}\right) + \left(\frac{2}{3}\right) = \frac{-5}{6}$$

2. Rational numbers are not commutative under subtraction.

Example :

$$\left(\frac{3}{4}\right) - \left(\frac{5}{2}\right) = \left(\frac{-7}{4}\right) \text{ and } \frac{5}{2} - \frac{3}{4} = \frac{7}{4}$$

$$\therefore \left(\frac{3}{4}\right) - \left(\frac{5}{2}\right) \neq \left(\frac{5}{2}\right) - \left(\frac{3}{4}\right)$$

3. Rational numbers are commutative under multiplication.

Example:

$$\left(\frac{3}{4}\right) \times \left(\frac{-2}{6}\right) = \left(\frac{-2}{6}\right) \times \left(\frac{3}{4}\right) = \frac{-1}{4}$$

4. Rational numbers are not commutative under division.

$$2 \div 5 \neq 5 \div 2$$

• **Associativity**

- Whole numbers are associative under addition and multiplication. However, they are **not** associative under subtraction and division.
- Integers are associative under addition and multiplication. However, they are **not** associative under subtraction and division.
- Rational numbers:

1. Rational numbers are associative under addition.

Example:

$$\left(\frac{2}{3} + \frac{1}{3}\right) + 1 = \frac{2}{3} + \left(\frac{1}{3} + 1\right) = 2$$

2. Rational numbers are **not** associative under subtraction.

Example:

$$\left(\frac{2}{3} - \frac{1}{3}\right) - 1 = \frac{-2}{3}$$

$$\frac{2}{3} - \left(\frac{1}{3} - 1\right) = \frac{4}{3}$$

$$\therefore \left(\frac{2}{3} - \frac{1}{3}\right) - 1 \neq \frac{2}{3} - \left(\frac{1}{3} - 1\right)$$

3. Rational numbers are associative under multiplication.

Example:

$$\left(\frac{2}{3} \times \frac{1}{3}\right) \times 1 = \frac{2}{3} \times \left(\frac{1}{3} \times 1\right) = \frac{2}{9}$$

4. Rational numbers are **not** associative under division.

Example:

$$\left\{\frac{2}{7} \div \left(\frac{-1}{14}\right)\right\} \div \frac{3}{7} = \frac{-28}{3}$$

$$\frac{2}{7} \div \left\{\left(\frac{-1}{14}\right) \div \frac{3}{7}\right\} = \frac{-12}{7}$$

$$\therefore \frac{2}{7} \div \left\{\left(\frac{-1}{14}\right)\right\} \div \frac{3}{7} \neq \frac{2}{7} \div \left\{\left(\frac{-1}{14}\right) \div \frac{3}{7}\right\}$$

- 0 is the additive identity of whole numbers, integers, and rational numbers.

$$\therefore 0 + a = a + 0 = a, \text{ where } a \text{ is a rational number}$$

- 1 is the multiplicative identity of whole numbers, integers, and rational numbers.

$$a \times 1 = 1 \times a = a$$

- Rational numbers are distributive over addition and subtraction.

$$\text{i.e., for any rational numbers } a, b, \text{ and } c, a(b + c) = ab + ac, a(b - c) = ab - ac$$

- Additive inverse of a number is the number, which when added to a number, gives 0. It is also called the negative of a number.

$$a + (-a) = (-a) + a = 0$$

$$\therefore \text{Additive inverse of } \frac{2}{5} \text{ is } \left(\frac{-2}{5}\right)$$

- Reciprocal or multiplicative inverse of a number is the number, which when multiplied by the number, gives 1. Therefore, the reciprocal of  $a$  is  $\frac{1}{a}$ .  $\left[a \times \frac{1}{a} = 1\right]$

$$\therefore \text{Reciprocal of } \frac{-2}{3} \text{ is } \frac{-3}{2}$$