

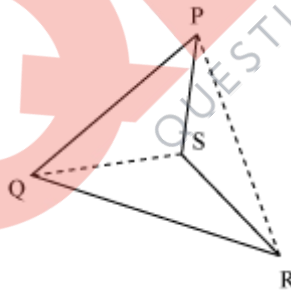
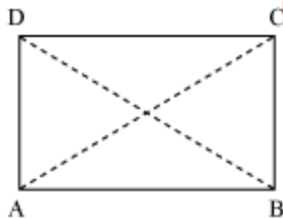
8th Standard-Maths

Understanding Quadrilaterals

- **Polygons**
 - A simple closed curve made up of line segments only is called a **polygon**.
 - **Polygons can be classified according to their number of sides (or vertices).**

Number of side/vertices	Classification
3	Triangle
4	Quadrilateral
5	Pentagon
6	Hexagon
7	Heptagon
.	.
.	.
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- The line segment connecting two non-consecutive vertices of a polygon are called **diagonals**.



For polygon ABCD, AC and BD are diagonals and for polygon PQRS, QS and PR are diagonals.

- The polygon, none of whose diagonals lie in its exterior, is called a **convex polygon**. In the given figure, ABCD is a convex polygon.

The polygon whose atleast one of the diagonals lie in its exterior is called a **concave polygon**. PQRS is a concave polygon.

- A polygon, which is both equiangular and equilateral, is called a **regular polygon**. Otherwise, it is an **irregular polygon**.

Example: Square is a regular polygon but rectangle is an irregular polygon.

- The sum of all the interior angles of an n -sided polygon is given by, $(n - 2) \times 180^\circ$.

Example: What is the number of sides of a polygon whose sum of all interior angles is 720° ?

Solution: It is known that,

$$(n - 2)180^\circ = 720^\circ$$

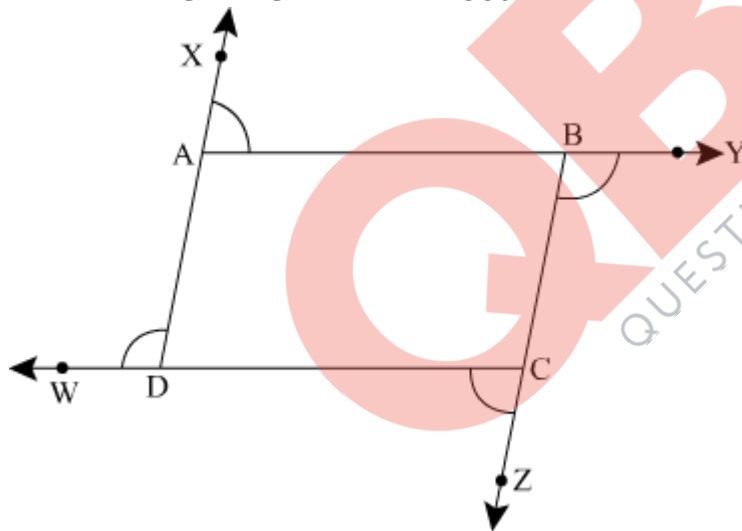
$$\Rightarrow (n - 2) = \frac{720^\circ}{180^\circ} = 4$$

$$\Rightarrow n = 6$$

Thus, the required polygon is six-sided.

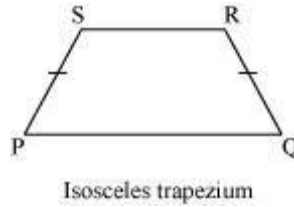
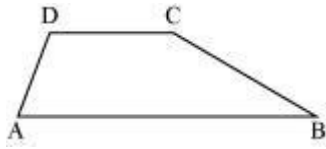
- The sum of measures of all exterior angles of a polygon is 360° .

For example, in the quadrilateral given below,
 $\angle XAB + \angle YBC + \angle ZCD + \angle WDA = 360^\circ$



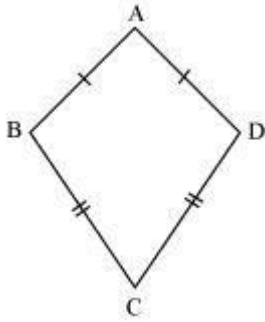
- **Trapezium**

- A quadrilateral with a pair of parallel sides is called a trapezium.
- A trapezium whose non-parallel sides are equal is called an isosceles trapezium.



- **Kite**

A kite is a quadrilateral with exactly two distinct consecutive pairs of sides of equal lengths.



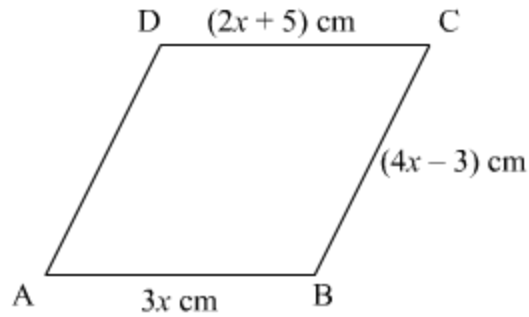
ABCD is a kite with $AB = AD$ and $BC = CD$.

- **Parallelogram**

1. A parallelogram is a quadrilateral whose opposite sides are parallel and equal.
 2. Its opposite angles are of equal measure.
 3. The adjacent angles in a parallelogram are supplementary.
 4. The diagonals of a parallelogram are not equal. However, they bisect each other.
- Opposite sides in a parallelogram are equal. Conversely, in a quadrilateral, if each pair of opposite sides are equal then the quadrilateral is a parallelogram.

Example:

In the following figure, ABCD is a parallelogram. Find the length of each sides.



Solution: We know, the opposite sides of a parallelogram are equal in length.

Therefore, $AB = CD$

$$3x = 2x + 5$$

$$\Rightarrow 3x - 2x = 5$$

$$\therefore x = 5$$

$$\text{Thus, } AB = 3x = 3 \times 5 = 15 \text{ cm}$$

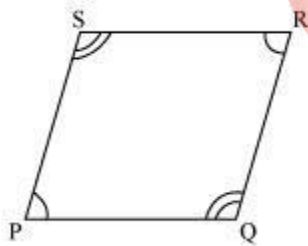
$$BC = 4x - 3 = 4 \times 5 - 3 = 17 \text{ cm}$$

$$CD = 2x + 5 = 2 \times 5 + 5 = 15 \text{ cm}$$

Also, $BC = AD$ [opposite sides of parallelogram]

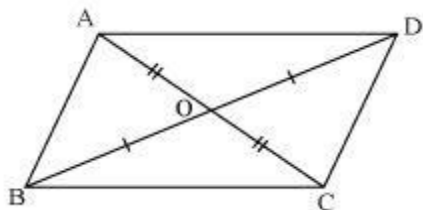
$$\therefore AD = 17 \text{ cm}$$

- In a parallelogram, opposite angles are equal. Conversely in a quadrilateral, if pair of opposite angles is equal, then the quadrilateral is a parallelogram.



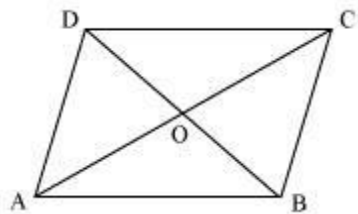
If in the quadrilateral PQRS, $\angle P = \angle R$ and $\angle Q = \angle S$ as shown in the above figure, then the quadrilateral is a parallelogram.

- The diagonals of a parallelogram bisect each other. Conversely, if the diagonals of a quadrilateral bisect each other, then it is a parallelogram.
Suppose ABCD is a quadrilateral. The diagonals of the quadrilateral intersect at O such that $AO = OC$ and $DO = OB$



Therefore, ABCD is a parallelogram.

Example: In the given figure, ABCD is a parallelogram. If $OD = (3x - 2)$ cm and $OB = (2x + 3)$ cm, then find x and length of diagonal BD.



Solution: We know that the diagonals of a parallelogram bisect each other.

$$\therefore OD = OB$$

$$\Rightarrow 3x - 2 = 2x + 3$$

$$\Rightarrow 3x - 2x = 3 + 2$$

$$\Rightarrow x = 5$$

Thus, the value of x is 5.

$$\text{Length of } BD = OD + OB$$

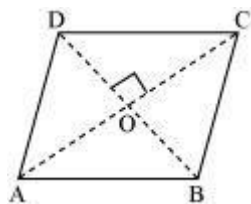
$$= (3x - 2) + (2x + 3)$$

$$= (3 \times 5 - 2) + (2 \times 5 + 3)$$

$$= 13 + 13$$

$$= 26 \text{ cm}$$

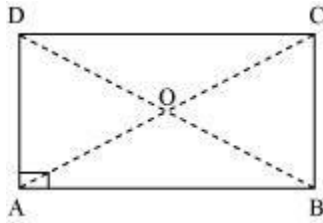
- **Rhombus:** A quadrilateral whose opposite sides are parallel and all sides are of equal lengths.
 - Its opposite angles are of equal measure.
 - Its diagonals are perpendicular bisectors of one another.



In rhombus ABCD, $OA = OC$ and $OB = OD$. Also, $AC \perp BD$.

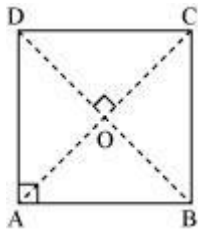
- A quadrilateral is a rhombus if its diagonals bisect each other at right angles.
- **Rectangle:** A parallelogram whose each interior angle is a right angle.

- Its diagonals are equal and bisect each other.



In rectangle ABCD, $AC = BD$. Also, $OA = OC$ and $OB = OD$

- A parallelogram is a rectangle if its diagonals are equal.
- **Square:** A square is a rectangle with equal sides.
- Its diagonals are equal and are perpendicular bisectors of each other.



In square ABCD, $AC = BD$ and $AC \perp BD$. Also, $OA = OC$ and $OB = OD$.

- A quadrilateral is a square, if its diagonals are equal and bisect each other at right angles.