



9	0 <b>OR</b> 3	1
10	$\hat{j}$	1
11	$\frac{1}{2} 2\hat{i} \times (-3\hat{j})  = \frac{1}{2} -6\hat{k}  = 3 \text{ sq units}$	1
12	$ \hat{a} + \hat{b} ^2 = 1$ $\Rightarrow \hat{a}^2 + \hat{b}^2 + 2\hat{a} \cdot \hat{b} = 1$ $\Rightarrow 2\hat{a} \cdot \hat{b} = 1 - 1 - 1$ $\Rightarrow \hat{a} \cdot \hat{b} = \frac{-1}{2} \Rightarrow  \hat{a}  \hat{b}  \cos \theta = \frac{-1}{2} \Rightarrow \theta = \pi - \frac{\pi}{3}$ $\Rightarrow \theta = \frac{2\pi}{3}$	1
13	1,0,0	1
14	(0,0,0)	1
15	$1 - \frac{2}{3} \times \frac{3}{4} = \frac{1}{2}$	1
16	$\left(\frac{1}{2}\right)^4 \left(\frac{1}{2}\right)^3 = \left(\frac{1}{2}\right)^7$	1
<b>Section II</b>		
17(i)	(b)	1
17(ii)	(a)	1
17(iii)	(c)	1
17(iv)	(a)	1
17(v)	(d)	1
18(i)	(b)	1
18(ii)	(c)	1
18(iii)	(b)	1
18(iv)	(d)	1
18(v)	(d)	1
<b>Section III</b>		
19	$\tan^{-1}\left(\frac{\cos x}{1-\sin x}\right) = \tan^{-1}\left[\frac{\sin\left(\frac{\pi}{2}-x\right)}{1-\cos\left(\frac{\pi}{2}-x\right)}\right]$ $\tan^{-1}\left[\frac{2\sin\left(\frac{\pi}{4}-\frac{x}{2}\right)\cos\left(\frac{\pi}{4}-\frac{x}{2}\right)}{2\sin^2\left(\frac{\pi}{4}-\frac{x}{2}\right)}\right]$	$\frac{1}{2}$



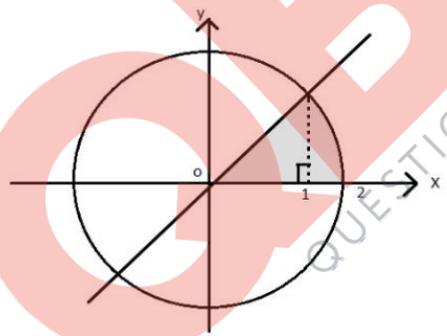
	$\therefore f(x) \text{ is continuous at } x = 0$ $\therefore \lim_{x \rightarrow 0} f(x) = f(0)$ $\Rightarrow \frac{k^2}{2} = \frac{1}{2} \Rightarrow k^2 = 1 \Rightarrow k = \pm 1$	$\frac{1}{2}$
22	$y = x + \frac{1}{x} \Rightarrow \frac{dy}{dx} = 1 - \frac{1}{x^2}$ <p><math>\therefore</math> normal is perpendicular to <math>3x - 4y = 7</math>, <math>\therefore</math> tangent is parallel to it</p> $1 - \frac{1}{x^2} = \frac{3}{4} \Rightarrow x^2 = 4 \Rightarrow x = 2 \quad (\because x > 0)$ <p>when <math>x = 2</math>, <math>y = 2 + \frac{1}{2} = \frac{5}{2}</math></p> <p><math>\therefore</math> Equation of Normal : <math>y - \frac{5}{2} = -\frac{4}{3}(x - 2) \Rightarrow 8x + 6y = 31</math></p>	1  1
23	$I = \int \frac{1}{\cos^2 x (1 - \tan x)^2} dx$ <p>Put, <math>1 - \tan x = y</math></p> <p>So that, <math>-\sec^2 x dx = dy</math></p> $= \int \frac{-1 dy}{y^2} = - \int y^{-2} dy$ $= + \frac{1}{y} + c = \frac{1}{1 - \tan x} + c$ <p style="text-align: center;"><b>OR</b></p> $I = \int_0^1 x (1 - x)^n dx$ $I = \int_0^1 (1 - x)[1 - (1 - x)]^n dx$ $I = \int_0^1 (1 - x) x^n dx = \int_0^1 (x^n - x^{n+1}) dx$ $I = \left[ \frac{x^{n+1}}{n+1} - \frac{x^{n+2}}{n+2} \right]_0^1$ $I = \left[ \left( \frac{1}{n+1} - \frac{1}{n+2} \right) - 0 \right] = \frac{1}{(n+1)(n+2)}$	1  1  $\frac{1}{2}$  1  $\frac{1}{2}$
24	$\text{Area} = 2 \int_0^2 \sqrt{8x} dx$ $= 2 \times 2\sqrt{2} \int_0^2 x^{\frac{1}{2}} dx$	1

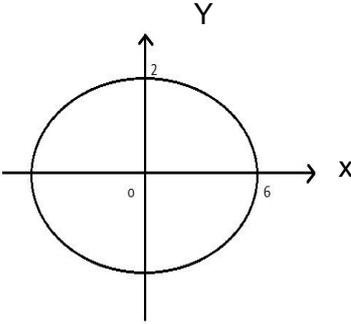


	<table border="1"> <tbody> <tr> <td>0</td> <td><math>\frac{4}{6} \times \frac{3}{5} = \frac{12}{30}</math></td> </tr> <tr> <td>1</td> <td><math>\left(\frac{2}{6} \times \frac{4}{5}\right) \times 2 = \frac{16}{30}</math></td> </tr> <tr> <td>2</td> <td><math>\frac{2}{6} \times \frac{1}{5} = \frac{2}{30}</math></td> </tr> </tbody> </table> <p>Most likely outcome is getting one chocolate of each type</p> <p align="center"><b>OR</b></p> <p><math>P(\bar{E}   \bar{F}) = P\left(\frac{\bar{E} \cap \bar{F}}{P(\bar{F})}\right) = \frac{P(\bar{E} \cup \bar{F})}{P(\bar{F})} = \frac{1 - P(E \cup F)}{1 - P(F)}</math>-----(1)</p> <p>Now <math>P(E \cup F) = P(E) + P(F) - P(E \cap F)</math>  <math>= 0.8 + 0.7 - 0.6 = 0.9</math></p> <p>Substituting value of <math>P(E \cup F)</math> in (1)</p> <p><math>P(\bar{E}   \bar{F}) = \frac{1 - 0.9}{1 - 0.7} = \frac{0.1}{0.3} = \frac{1}{3}</math></p>	0	$\frac{4}{6} \times \frac{3}{5} = \frac{12}{30}$	1	$\left(\frac{2}{6} \times \frac{4}{5}\right) \times 2 = \frac{16}{30}$	2	$\frac{2}{6} \times \frac{1}{5} = \frac{2}{30}$	<p align="right"><math>1\frac{1}{2}</math></p> <p align="right"><math>\frac{1}{2}</math></p> <p align="right">1</p> <p align="right"><math>\frac{1}{2}</math></p> <p align="right"><math>\frac{1}{2}</math></p>
0	$\frac{4}{6} \times \frac{3}{5} = \frac{12}{30}$							
1	$\left(\frac{2}{6} \times \frac{4}{5}\right) \times 2 = \frac{16}{30}$							
2	$\frac{2}{6} \times \frac{1}{5} = \frac{2}{30}$							
	<b>Section IV</b>							
29	<p>(i) Reflexive :                  Since, <math>a+a=2a</math> which is even <math>\therefore (a,a) \in R \forall a \in Z</math>                  Hence R is reflexive</p> <p>(ii) Symmetric:                  If <math>(a,b) \in R</math>, then <math>a+b = 2\lambda \Rightarrow b+a = 2\lambda</math>  <math>\Rightarrow (b,a) \in R</math>, Hence R is symmetric</p> <p>(iii) Transitive:                  If <math>(a,b) \in R</math> and <math>(b,c) \in R</math>                  then <math>a+b = 2\lambda</math>---(1) and <math>b+c = 2\mu</math> ---- (2)                  Adding (1) and (2) we get  <math>a+2b+c=2(\lambda + \mu)</math>  <math>\Rightarrow a+c=2(\lambda + \mu - b)</math>  <math>\Rightarrow a+c=2k</math>, where <math>\lambda + \mu - b = k \Rightarrow (a,c) \in R</math>                  Hence R is transitive  <math>[0] = \{\dots-4, -2, 0, 2, 4\dots\}</math></p>	<p align="right"><math>\frac{1}{2}</math></p> <p align="right">1</p> <p align="right"><math>\frac{1}{2}</math></p> <p align="right"><math>\frac{1}{2}</math></p>						
30	Let $u = e^{x \sin^2 x}$ and $v = (\sin x)^x$	$\frac{1}{2}$						

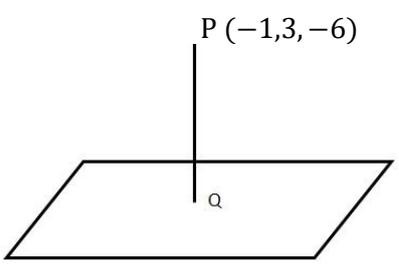
	<p>so that <math>y = u + v \Rightarrow \frac{dy}{dx} = \frac{du}{dx} + \frac{dv}{dx}</math>-----(1)</p> <p>Now, <math>u = e^{x \sin^2 x}</math> , Differentiating both sides w.r.t. x, we get</p> $\Rightarrow \frac{du}{dx} = e^{x \sin^2 x} [x(\sin 2x) + \sin^2 x] \quad \text{----- (2)}$ <p>Also , <math>v = (\sin x)^x</math></p> $\Rightarrow \log v = x \log (\sin x)$ <p>Differentiating both sides w.r.t. x, we get</p> $\frac{1}{v} \frac{dv}{dx} = x \cot x + \log (\sin x)$ $\frac{dv}{dx} = (\sin x)^x [x \cot x + \log(\sin x)] \quad \text{----- (3)}$ <p>Substituting from – (2), – (3) in – (1) we get</p> $\frac{dy}{dx} = e^{x \sin^2 x} [x \sin 2x + \sin^2 x] + (\sin x)^x [x \cot x + \log(\sin x)]$	<p align="center">1</p> <p align="center">1</p> <p align="center"><math>\frac{1}{2}</math></p>
<p>31</p>	$\text{RHD} = \lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h} = \lim_{h \rightarrow 0} \frac{[1+h] - [1]}{h}$ $= \lim_{h \rightarrow 0} \frac{(1-1)}{h} = 0$ $\text{LHD} = \lim_{h \rightarrow 0} \frac{f(1-h) - f(1)}{-h} = \lim_{h \rightarrow 0} \frac{[1-h] - [1]}{-h} = \lim_{h \rightarrow 0} \frac{0-1}{-h}$ $= \lim_{h \rightarrow 0} \frac{1}{h} = \infty$ <p>Since, RHD <math>\neq</math> LHD Therefore <math>f(x)</math> is not differentiable at <math>x = 1</math></p> <p align="center"><b>OR</b></p> $y = b \tan \theta \Rightarrow \frac{dy}{d\theta} = b \sec^2 \theta \dots (1)$ $x = a \sec \theta \Rightarrow \frac{dx}{d\theta} = a \sec \theta \tan \theta \dots (2)$	<p align="center">1</p> <p align="center">1</p> <p align="center">1</p>

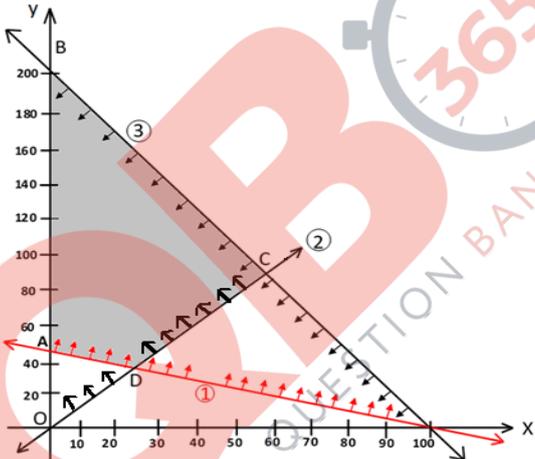
	$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{b \sec^2 \theta}{a \sec \theta \tan \theta} = \frac{b}{a} \operatorname{cosec} \theta$ <p><i>Differentiating both sides w.r.t. x, we get</i></p> $\begin{aligned} \frac{d^2y}{dx^2} &= \frac{-b}{a} \operatorname{cosec} \theta \cot \theta \times \frac{d\theta}{dx} \\ &= \frac{-b}{a} \operatorname{cosec} \theta \cot \theta \times \frac{1}{a \sec \theta \tan \theta} \quad [\text{using (2)}] \\ &= \frac{-b}{a.a} \cot^3 \theta \end{aligned}$ $\left. \frac{d^2y}{dx^2} \right _{\theta=\frac{\pi}{6}} = \frac{-b}{a} \left[ \cot \frac{\pi}{6} \right]^3 = \frac{-b}{a} (\sqrt{3})^3 = -\frac{3\sqrt{3}b}{a.a}$	$1\frac{1}{2}$          $\frac{1}{2}$
32	$f(x) = \tan x - 4x$ $f'(x) = \sec^2 x - 4$ <p>a) For <math>f(x)</math> to be strictly increasing</p> $f'(x) > 0$ $\Rightarrow \sec^2 x - 4 > 0$ $\Rightarrow \sec^2 x > 4$ $\Rightarrow \cos^2 x < \frac{1}{4} \Rightarrow \cos^2 x < \left(\frac{1}{2}\right)^2$ $\Rightarrow -\frac{1}{2} < \cos x < \frac{1}{2} \Rightarrow \frac{\pi}{3} < x < \frac{\pi}{2}$ <p>b) For <math>f(x)</math> to be strictly decreasing</p> $f'(x) < 0$ $\Rightarrow \sec^2 x - 4 < 0$ $\Rightarrow \sec^2 x < 4$ $\Rightarrow \cos^2 x > \frac{1}{4}$ $\Rightarrow \cos^2 x > \left(\frac{1}{2}\right)^2$ $\Rightarrow \cos x > \frac{1}{2} \left[ \because x \in \left(0, \frac{\pi}{2}\right) \right]$ $\Rightarrow 0 < x < \frac{\pi}{3}$	$\frac{1}{2}$          $1\frac{1}{2}$          1

<p>33</p>	<p>Put <math>x^2 = y</math> to make partial fractions</p> $\frac{x^2 + 1}{(x^2 + 2)(x^2 + 3)} = \frac{y + 1}{(y + 2)(y + 3)} = \frac{A}{y + 2} + \frac{B}{y + 3}$ $\Rightarrow y + 1 = A(y + 3) + B(y + 2) \dots \dots \dots (1)$ <p>Comparing coefficients of y and constant terms on both sides of (1) we get</p> <p align="center"><math>A + B = 1</math> and <math>3A + 2B = 1</math></p> <p align="center">Solving, we get <math>A = -1, B = 2</math></p> $\int \frac{x^2 + 1}{(x^2 + 2)(x^2 + 3)} dx = \int \frac{-1}{x^2 + 2} dx + 2 \int \frac{1}{x^2 + 3} dx$ $= -\frac{1}{\sqrt{2}} \tan^{-1} \left( \frac{x}{\sqrt{2}} \right) + \frac{2}{\sqrt{3}} \tan^{-1} \left( \frac{x}{\sqrt{3}} \right) + C$	<p align="center"><math>\frac{1}{2}</math></p> <p align="center"><math>\frac{1}{2}</math></p> <p align="center">1</p> <p align="center">1</p>
<p>34</p>	<p>Solving <math>y = \sqrt{3}x</math> and <math>x^2 + y^2 = 4</math></p> <p>We get <math>x^2 + 3x^2 = 4</math></p> <p><math>\Rightarrow x^2 = 1 \Rightarrow x = 1</math></p>  <p>Required Area</p> $= \sqrt{3} \int_0^1 x dx + \int_1^2 \sqrt{2^2 - x^2} dx$ $= \frac{\sqrt{3}}{2} [x^2]_0^1 + \left[ \frac{x}{2} \sqrt{2^2 - x^2} + 2 \sin^{-1} \left( \frac{x}{2} \right) \right]_1^2$ $= \frac{\sqrt{3}}{2} + \left[ 2 \times \frac{\pi}{2} - \frac{\sqrt{3}}{2} - 2 \times \frac{\pi}{6} \right]$ <p><math>\frac{2\pi}{3}</math> sq units</p> <p align="center"><b>OR</b></p>	<p align="center"><math>\frac{1}{2}</math></p> <p align="center"><math>\frac{1}{2}</math></p> <p align="center">1</p> <p align="center"><math>\frac{1}{2}</math></p>

	<p>Required Area = <math>\frac{4}{3} \int_0^6 \sqrt{6^2 - x^2} dx</math></p>  <p> <math display="block">= \frac{4}{3} \left[ \frac{x}{2} \sqrt{6^2 - x^2} + 18 \sin^{-1} \left( \frac{x}{6} \right) \right]_0^6</math> <math display="block">= \frac{4}{3} \left[ 18 \times \frac{\pi}{2} - 0 \right] = 12\pi \text{ sq units}</math> </p>	<p align="center"><math>\frac{1}{2}</math></p> <p align="center"><math>\frac{1}{2}</math></p> <p align="center">1</p> <p align="center">1</p>
<p>35</p>	<p>The given differential equation can be written as</p> $\frac{dy}{dx} = \frac{y + 2x^2}{x} \Rightarrow \frac{dy}{dx} - \frac{1}{x}y = 2x$ <p>Here <math>P = -\frac{1}{x}</math>, <math>Q = 2x</math></p> $\text{IF} = e^{\int P dx} = e^{-\int \frac{1}{x} dx} = e^{-\log x} = \frac{1}{x}$ <p>The solutions is :</p> $y \times \frac{1}{x} = \int \left( 2x \times \frac{1}{x} \right) dx$ $\Rightarrow \frac{y}{x} = 2x + c$ $\Rightarrow y = 2x^2 + cx$	<p align="center"><math>\frac{1}{2}</math></p> <p align="center">1</p> <p align="center">1</p> <p align="center"><math>\frac{1}{2}</math></p>
<p>36</p>	<p><math> A  = 1(-1 - 2) - 2(-2 - 0) = -3 + 4 = 1</math></p> <p>A is nonsingular, therefore <math>A^{-1}</math> exists</p> $\text{Adj } A = \begin{bmatrix} -3 & -2 & -4 \\ 2 & 1 & 2 \\ 2 & 1 & 3 \end{bmatrix}$ $\Rightarrow A^{-1} = \frac{1}{ A } (\text{Adj } A) = \begin{bmatrix} -3 & -2 & -4 \\ 2 & 1 & 2 \\ 2 & 1 & 3 \end{bmatrix}$	<p align="center"><math>\frac{1}{2}</math></p> <p align="center"><math>1\frac{1}{2}</math></p>

	<p>The given equations can be written as:</p> $\begin{bmatrix} 1 & -2 & 0 \\ 2 & -1 & -1 \\ 0 & -2 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix}$ <p>Which is of the form <math>A'X = B</math></p> $\Rightarrow X = (A')^{-1}B = (A^{-1})'B$ $\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -3 & 2 & 2 \\ -2 & 1 & 1 \\ -4 & 2 & 3 \end{bmatrix} \begin{bmatrix} 10 \\ 8 \\ 7 \end{bmatrix} = \begin{bmatrix} 0 \\ -5 \\ -3 \end{bmatrix}$ $\Rightarrow x = 0, \quad y = -5, \quad z = -3$ <p style="text-align: center;"><b>OR</b></p> $AB = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix}$ $= \begin{bmatrix} 6 & 0 & 0 \\ 0 & 6 & 0 \\ 0 & 0 & 6 \end{bmatrix}$ $\Rightarrow AB = 6I$ $\Rightarrow A\left(\frac{1}{6}B\right) = I \Rightarrow A^{-1} = \frac{1}{6}(B)$ <p>The given equations can be written as</p> $\begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 3 \\ 17 \\ 7 \end{bmatrix}$ $AX = D, \text{ where } D = \begin{bmatrix} 3 \\ 17 \\ 7 \end{bmatrix}$ $\Rightarrow X = A^{-1}D$ $\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix} \begin{bmatrix} 3 \\ 17 \\ 7 \end{bmatrix} = \frac{1}{6} \begin{bmatrix} 12 \\ -6 \\ 24 \end{bmatrix}$ $\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 4 \end{bmatrix}$ $x = 2, \quad y = -1, \quad z = 4$	<p><math>\frac{1}{2}</math></p> <p>1</p> <p><math>1\frac{1}{2}</math></p> <p><math>1\frac{1}{2}</math></p> <p>1</p> <p>1</p> <p><math>1\frac{1}{2}</math></p>
37	We have $a_1 = 3\hat{i} + 2\hat{j} - 4\hat{k}$ $b_1 = \hat{i} + 2\hat{j} + 2\hat{k}$	

$a_2 = 5i - 2j$ $b_2 = 3i + 2j + 6k$ $\vec{a}_2 - \vec{a}_1 = 2i - 4j + 4k$ $\vec{b}_1 \times \vec{b}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 2 \\ 3 & 2 & 6 \end{vmatrix} = i(12 - 4) - j(6 - 6) + k(2 - 6)$ $\vec{b}_1 \times \vec{b}_2 = 8i + 0j - 4k = 8i - 4k$ $\therefore (\vec{b}_1 \times \vec{b}_2) \cdot (\vec{a}_2 - \vec{a}_1) = 16 - 16 = 0$ <p><math>\therefore</math> The lines are intersecting and the shortest distance between the lines is 0.</p> <p>Now for point of intersection</p> $3i + 2j - 4k + \lambda(i + 2j + 2k) = 5i - 2j + \mu(3i + 2j + 6k)$ $\Rightarrow 3 + \lambda = 5 + 3\mu \quad \text{--- (1)}$ $2 + 2\lambda = -2 + 2\mu \quad \text{--- (2)}$ $-4 + 2\lambda = 6\mu \quad \text{--- (3)}$ <p>Solving (1) and (2) we get, <math>\mu = -2</math> and <math>\lambda = -4</math></p> <p>Substituting in equation of line we get</p> $\vec{r} = 5i - 2j + (-2)(3i + 2j - 6k) = -i - 6j - 12k$ <p>Point of intersection is <math>(-1, -6, -12)</math></p> <p style="text-align: center;"><b>OR</b></p> <p>Let P be the given point and Q be the foot of the perpendicular.</p> <p>Equation of PQ <math>\frac{x+1}{2} = \frac{y-3}{1} = \frac{z+6}{-2} = \lambda</math></p> <div style="text-align: center;">  </div> <p>Let coordinates of Q be <math>(2\lambda - 1, \lambda + 3, -2\lambda - 6)</math></p> <p>Since Q lies in the plane <math>2x + y - 2z + 5 = 0</math></p> $\therefore 2(2\lambda - 1) + (\lambda + 3) - 2(-2\lambda - 6) + 5 = 0$ $\Rightarrow 4\lambda - 2 + \lambda + 3 + 4\lambda + 12 + 5 = 0$	<p>1</p> <p>1</p> <p>1</p> <p>1</p> <p>1</p> <p><math>1\frac{1}{2}</math></p> <p><math>\frac{1}{2}</math></p>
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	$\Rightarrow 9\lambda + 18 = 0 \quad \Rightarrow \lambda = -2$ <p align="center"><math>\therefore</math> coordinates of Q are (-5, 1, -2)</p> <p>Length of the perpendicular = <math>\sqrt{(-5 + 1)^2 + (1 - 3)^2 + (-2 + 6)^2}</math></p> <p align="center">= 6 units</p>	<p align="center">1</p> <p align="center">1</p> <p align="center">1</p>																						
<p>38</p>	<p>Max <math>Z = 3x + y</math></p> <p>Subject to</p> <table style="margin-left: 40px;"> <tr> <td><math>x + 2y \geq 100</math></td> <td>-----</td> <td>(1)</td> </tr> <tr> <td><math>2x - y \leq 0</math></td> <td>-----</td> <td>(2)</td> </tr> <tr> <td><math>2x + y \leq 200</math></td> <td>-----</td> <td>(3)</td> </tr> <tr> <td><math>x \geq 0, \quad y \geq 0</math></td> <td></td> <td></td> </tr> </table>  <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Corner Points</th> <th><math>Z = 3x + y</math></th> </tr> </thead> <tbody> <tr> <td>A (0, 50)</td> <td>50</td> </tr> <tr> <td>B (0, 200)</td> <td>200</td> </tr> <tr> <td>C (50, 100)</td> <td>250</td> </tr> <tr> <td>D (20, 40)</td> <td>100</td> </tr> </tbody> </table> <p align="center"><math>Max z = 250</math> at <math>x = 50, \quad y = 100</math></p>	$x + 2y \geq 100$	-----	(1)	$2x - y \leq 0$	-----	(2)	$2x + y \leq 200$	-----	(3)	$x \geq 0, \quad y \geq 0$			Corner Points	$Z = 3x + y$	A (0, 50)	50	B (0, 200)	200	C (50, 100)	250	D (20, 40)	100	<p align="center">3</p> <p align="center">1</p> <p align="center">1</p>
$x + 2y \geq 100$	-----	(1)																						
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D (20, 40)	100																							

OR																
(i)	<table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 5px;">Corner points</th> <th style="padding: 5px;"><math>Z = 3x - 4y</math></th> </tr> </thead> <tbody> <tr> <td style="padding: 5px;">O(0,0)</td> <td style="padding: 5px;">0</td> </tr> <tr> <td style="padding: 5px;">A(0,8)</td> <td style="padding: 5px;">-32</td> </tr> <tr> <td style="padding: 5px;">B(4,10)</td> <td style="padding: 5px;">-28</td> </tr> <tr> <td style="padding: 5px;">C(6,8)</td> <td style="padding: 5px;">-14</td> </tr> <tr> <td style="padding: 5px;">D(6,5)</td> <td style="padding: 5px;">-2</td> </tr> <tr> <td style="padding: 5px;">E(4,0)</td> <td style="padding: 5px;">12</td> </tr> </tbody> </table> <p style="margin: 5px auto; text-align: center;"> <math>Max\ Z = 12\ at\ E(4,0)</math>  <math>Min\ Z = -32\ at\ A(0,8)</math> </p>	Corner points	$Z = 3x - 4y$	O(0,0)	0	A(0,8)	-32	B(4,10)	-28	C(6,8)	-14	D(6,5)	-2	E(4,0)	12	$1\frac{1}{2}$
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(ii)	<p>Since maximum value of Z occurs at B(4,10) and C(6, 8)</p> <p><math>\therefore 4p + 10q = 6p + 8q</math></p> <p><math>\Rightarrow 2q = 2p</math></p> <p><math>\Rightarrow p = q</math></p> <p>Number of optimal solution are infinite</p>	<p>1</p> <p><math>\frac{2}{1}</math></p> <p><math>\frac{1}{2}</math></p>														

