

# QB365 Question Bank Software

## 12th Maths CBSE Case Study Application of Integrals Questions For - 2024

12th Standard

Maths

### SECTION-A

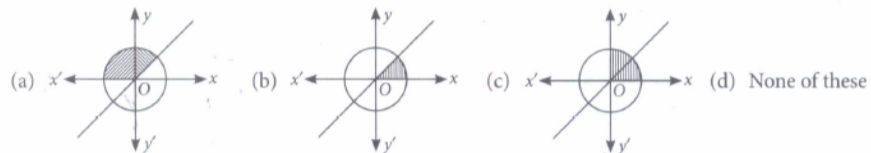
2 x 4 = 8

1) Consider the curve  $x^2 + y^2 = 16$  and line  $y = x$  in the first quadrant. Based on the above information, answer the following questions.

(i) Point of intersection of both the given curves is

- (a)  $(0, 4)$       (b)  $(0, 2\sqrt{2})$       (c)  $(2\sqrt{2}, 2\sqrt{2})$       (d)  $(2\sqrt{2}, 4)$

(ii) Which of the following shaded portion represent the area bounded by given two curves?



(iii) The value of the integral  $\int_0^{2\sqrt{2}} x dx$  is

- (a) 0      (b) 1      (c) 2      (d) 4

(iv) The value of the integral  $\int_{2\sqrt{2}}^4 \sqrt{16 - x^2} dx$  is

- (a)  $2(\pi - 2)$       (b)  $2(\pi - 8)$       (c)  $4(\pi - 2)$       (d)  $4(\pi + 2)$

(v) Area bounded by the two given curves is

- (a)  $3\pi$  sq. units      (b)  $\frac{\pi}{2}$  sq. units      (c)  $\pi$  sq. units      (d)  $2\pi$  sq. units

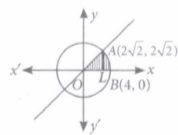
**Answer : (i) (c) :** We have,  $x^2 + y^2 = 16$  ..(i)

and  $y = x$  ...(ii)

From (i) and (ii),  $2x^2 = 16 \Rightarrow x^2 = 8 \Rightarrow x = 2\sqrt{2}$  ( $\because$  x lies in first quadrant)

$\therefore$  Point of intersection of (i) and (ii) in first quadrant is  $(2\sqrt{2}, 2\sqrt{2})$ .

**(ii) (b) :** The shaded region which represent the area bounded by two given curves in first quadrant is shown below.



$$\text{(iii) (d) : } \int_0^{2\sqrt{2}} x dx = \left[ \frac{x^2}{2} \right]_0^{2\sqrt{2}} = \frac{(2\sqrt{2})^2}{2} = \frac{8}{2} = 4$$

$$\begin{aligned} \text{(iv) (a) : } \int_{2\sqrt{2}}^4 \sqrt{16 - x^2} dx &= \left[ \frac{x}{2} \sqrt{16 - x^2} + \frac{16}{2} \cdot \sin^{-1} \left( \frac{x}{4} \right) \right]_{2\sqrt{2}}^4 \\ &= 8 \sin^{-1}(1) - 4 - 8 \sin^{-1} \left( \frac{1}{\sqrt{2}} \right) \end{aligned}$$

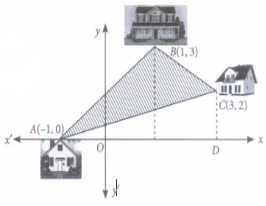
$$= 8 \left( \frac{\pi}{2} \right) - 4 - 8 \left( \frac{\pi}{4} \right) = 4\pi - 4 - 2\pi = 2\pi - 4 = 2(\pi - 2)$$

**(v) (d) :** Required area = Area (OLA) + Area (BAL)

$$= \int_0^{2\sqrt{2}} x dx + \int_{2\sqrt{2}}^4 \sqrt{16 - x^2} dx$$

$$= 4 + 2(\pi - 2) = 2\pi \text{ sq. units.}$$

2) Location of three houses of a society is represented by the points A(-1, 0), B(1, 3) and C(3, 2) as shown in figure. Based on the above information, answer the following questions



(i) Equation of line AB is

(a)  $y = \frac{3}{2}(x + 1)$       (b)  $y = \frac{3}{2}(x - 1)$       (c)  $y = \frac{1}{2}(x + 1)$       (d)  $y = \frac{1}{2}(x - 1)$

(ii) Equation of line BC is

(a)  $y = \frac{1}{2}x - \frac{7}{2}$       (b)  $y = \frac{3}{2}x - \frac{7}{2}$       (c)  $y = -\frac{1}{2}x + \frac{7}{2}$       (d)  $y = \frac{3}{2}x + \frac{7}{2}$

(iii) Area of region ABCD is

(a) 2 sq. units      (b) 4 sq. units      (c) 6 sq. units      (d) 8 sq. units

(iv) Area of  $\triangle ADC$  is

(a) 4 sq. units      (b) 8 sq. units      (c) 16 sq. units      (d) 32 sq. units

(v) Area of  $\triangle ABC$  is

(a) 3 sq. units      (b) 4 sq. units      (c) 5 sq. units      (d) 6 sq. units

**Answer :** (i) (a) : Equation of line AB is

$$y - 0 = \frac{3-0}{1+1}(x + 1) \Rightarrow y = \frac{3}{2}(x + 1)$$

(ii) (c) : Equation of line BC is  $y - 3 = \frac{2-3}{3-1}(x - 1)$

$$\Rightarrow y = -\frac{1}{2}x + \frac{1}{2} + 3 \Rightarrow y = -\frac{1}{2}x + \frac{7}{2}$$

(iii) (d) : Area of region ABCD

= Area of  $\triangle ABE$  + Area of region BCDE

$$= \int_{-1}^1 \frac{3}{2}(x + 1)dx + \int_1^3 \left(-\frac{1}{2}x + \frac{7}{2}\right) dx$$

$$= \frac{3}{2} \left[ \frac{x^2}{2} + x \right]_{-1}^1 + \left[ -\frac{x^2}{4} + \frac{7}{2}x \right]_1^3$$

$$= \frac{3}{2} \left[ \frac{1}{2} + 1 - \frac{1}{2} + 1 \right] + \left[ -\frac{9}{4} + \frac{21}{2} + \frac{1}{4} - \frac{7}{2} \right]$$

$$= 3 + 5 = 8 \text{ sq. units}$$

(iv) (a) : Equation of line AC is  $y - 0 = \frac{2-0}{3+1}(x + 1)$

$$\Rightarrow y = \frac{1}{2}(x + 1)$$

$$\therefore \text{Area of } \triangle ADC = \int_{-1}^3 \frac{1}{2}(x + 1)dx = \left[ \frac{x^2}{4} + \frac{1}{2}x \right]_{-1}^3$$

$$= \frac{9}{4} + \frac{3}{2} - \frac{1}{4} + \frac{1}{2} = 4 \text{ sq. units}$$

(v) (b) : Area of  $\triangle ABC$  = Area of region ABCD - Area of  $\triangle ADC$  =  $8 - 4 = 4$  sq. units