

# QB365 Question Bank Software Study Materials

## Complex Numbers 50 Important 1Marks Questions With Answers (Book Back and Creative)

12th Standard

Maths

Total Marks : 50

50 x 1 = 50

- 1)  $i^n + i^{n+1} + i^{n+2} + i^{n+3}$  is  
**(a) 0** (b) 1 (c) -1 (d) i
- 2) The value of  $\sum_{n=1}^{13} (i^n + i^{n-1})$  is  
**(a) 1 + i** (b) i (c) 1 (d) 0
- 3) The area of the triangle formed by the complex numbers  $z$ ,  $iz$  and  $z+iz$  in the Argand's diagram is  
**(a)  $\frac{1}{2}|z|^2$**  (b)  $|z|^2$  (c)  $\frac{3}{2}|z|^2$  (d)  $2|z|^2$
- 4) The conjugate of a complex number is  $\frac{1}{i-2}$ . Then the complex number is  
**(a)  $\frac{1}{i+2}$**  **(b)  $\frac{-1}{i+2}$**  (c)  $\frac{-1}{i-2}$  (d)  $\frac{1}{i-2}$
- 5) If  $z = \frac{(\sqrt{3} + i)^3 (3i + 4)^2}{(8 + 6i)^2}$ , then  $|z|$  is equal to  
**(a) 0** (b) 1 **(c) 2** (d) 3
- 6) If  $z$  is a non zero complex number, such that  $2iz^2 = \bar{z}$  then  $|z|$  is  
**(a)  $\frac{1}{2}$**  (b) 1 (c) 2 (d) 3
- 7) If  $|z - 2 + i| \leq 2$ , then the greatest value of  $|z|$  is  
**(a)  $\sqrt{3} - 2$**  (b)  $\sqrt{3} + 2$  (c)  $\sqrt{5} - 2$  **(d)  $\sqrt{5} + 2$**
- 8) If  $|z - \frac{3}{z}| = 2$ , then the least value  $|z|$  is  
**(a) 1** (b) 2 (c) 3 (d) 5
- 9) If  $|z| = 1$ , then the value of  $\frac{1+z}{1+\bar{z}}$  is  
**(a) z** (b)  $\bar{z}$  (c)  $\frac{1}{z}$  (d) 1
- 10) The solution of the equation  $|z| - z = 1 + 2i$  is  
**(a)  $\frac{3}{2} - 2i$**  (b)  $-\frac{3}{2} + 2i$  (c)  $2 - \frac{3}{2}i$  (d)  $2 + \frac{3}{2}i$
- 11) If  $|z_1| = 1$ ,  $|z_2| = 2$ ,  $|z_3| = 3$  and  $|9z_1z_2 + 4z_1z_3 + z_2z_3| = 12$ , then the value of  $|z_1 + z_2 + z_3|$  is  
**(a) 1** **(b) 2** (c) 3 (d) 4
- 12) If  $z$  is a complex number such that  $z \in \mathbb{C} \setminus \mathbb{R}$  and  $z + \frac{1}{z} \in \mathbb{R}$ , then  $|z|$  is  
**(a) 0** **(b) 1** (c) 2 (d) 3
- 13)  $z_1, z_2$  and  $z_3$  are complex number such that  $z_1 + z_2 + z_3 = 0$  and  $|z_1| = |z_2| = |z_3| = 1$  then  $z_1^2 + z_2^2 + z_3^3$  is

- (a) 3 (b) 2 (c) 1 **(d) 0**
- 14) If  $\frac{z-1}{z+1}$  is purely imaginary, then  $|z|$  is  
 (a)  $\frac{1}{2}$  **(b) 1** (c) 2 (d) 3
- 15) If  $z = x + iy$  is a complex number such that  $|z+2| = |z-2|$ , then the locus of  $z$  is  
 (a) real axis **(b) imaginary axis** (c) ellipse (d) circle
- 16) The principal argument of  $\frac{3}{-1+i}$  is  
 (a)  $-\frac{5\pi}{6}$  (b)  $-\frac{2\pi}{3}$  **(c)  $-\frac{3\pi}{4}$**  (d)  $-\frac{\pi}{2}$
- 17) The principal argument of  $(\sin 40^\circ + i \cos 40^\circ)^5$  is  
**(a)  $-110^\circ$**  (b)  $-70^\circ$  (c)  $70^\circ$  (d)  $110^\circ$
- 18) If  $(1+i)(1+2i)(1+3i)\dots(1+ni) = x + iy$ , then  $2 \cdot 5 \cdot 10 \dots (1+n^2)$  is  
 (a) 1 (b)  $i$  **(c)  $x^2+y^2$**  (d)  $1+n^2$
- 19) If  $\omega \neq 1$  is a cubic root of unity and  $(1+\omega)^7 = A + B\omega$ , then  $(A, B)$  equals  
 (a)  $(1, 0)$  (b)  $(-1, 1)$  (c)  $(0, 1)$  **(d)  $(1, 1)$**
- 20) The principal argument of the complex number  $\frac{(1+i\sqrt{3})^2}{4i(1-i\sqrt{3})}$  is  
 (a)  $\frac{2\pi}{3}$  (b)  $\frac{\pi}{6}$  (c)  $\frac{5\pi}{6}$  **(d)  $\frac{\pi}{2}$**
- 21) If  $\alpha$  and  $\beta$  are the roots of  $x^2+x+1 = 0$ , then  $\alpha^{2020} + \beta^{2020}$  is  
 (a) -2 **(b) -1** (c) 1 (d) 2
- 22) The product of all four values of  $\left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}\right)^{\frac{3}{4}}$  is  
 (a) -2 (b) -1 **(c) 1** (d) 2
- 23) If  $\omega \neq 1$  is a cubic root of unity and  $\begin{vmatrix} 1 & 1 & 1 \\ 1 & -\omega^2 - 1 & \omega^2 \\ 1 & \omega^2 & \omega^7 \end{vmatrix} = 3k$ , then  $k$  is equal to  
 (a) 1 (b) -1 (c)  $\sqrt{3i}$  **(d)  $-\sqrt{3i}$**
- 24) The value of  $\left(\frac{1+\sqrt{3}i}{1-\sqrt{3}i}\right)^{10}$  is  
**(a)  $cis \frac{2\pi}{3}$**  (b)  $cis \frac{4\pi}{3}$  (c)  $-cis \frac{2\pi}{3}$  (d)  $-cis \frac{4\pi}{3}$
- 25) If  $\omega = cis \frac{2\pi}{3}$ , then the number of distinct roots of  $\begin{vmatrix} z+1 & \omega & \omega^2 \\ \omega & z+\omega^2 & 1 \\ \omega^2 & 1 & z+\omega \end{vmatrix} = 0$   
**(a) 1** (b) 2 (c) 3 (d) 4
- 26) If  $\sqrt{a+ib} = x + iy$ , then possible value of  $\sqrt{a-ib}$  is \_\_\_\_\_  
 (a)  $x^2+y^2$  (b)  $\sqrt{x^2+y^2}$  (c)  $x+iy$  **(d)  $x-iy$**
- 27) If,  $i^2 = -1$ , then  $i^1 + i^2 + i^3 + \dots$  up to 1000 terms is equal to \_\_\_\_\_  
 (a) 1 (b) -1 (c)  $i$  **(d) 0**
- 28) If  $z = \cos \frac{\pi}{4} + i \sin \frac{\pi}{6}$ , then \_\_\_\_\_

(a)  $|z| = 1, \arg(z) = \frac{\pi}{4}$    (b)  $|z| = 1, \arg(z) = \frac{\pi}{6}$    (c)  $|z| = \frac{\sqrt{3}}{2}, \arg(z) = \frac{5\pi}{24}$    **(d)  $|z| = \frac{\sqrt{3}}{2}, \arg(z) = \tan^{-1}\left(\frac{1}{\sqrt{2}}\right)$**

29) The least positive integer  $n$  such that  $\left(\frac{2i}{1+i}\right)^n$  is a positive integer is \_\_\_\_\_

- (a) 16   **(b) 8**   (c) 4   (d) 2

30) If  $z = \frac{1}{1 - \cos\theta - i\sin\theta}$ , the  $\operatorname{Re}(z) =$  \_\_\_\_\_

- (a) 0   **(b)  $\frac{1}{2}$**    (c)  $\cot\frac{\theta}{2}$    (d)  $\frac{1}{2} \cot\frac{\theta}{2}$

31) The complex number  $z$  which satisfies the condition  $\left|\frac{1+z}{1-z}\right| = 1$  lies on \_\_\_\_\_

- (a) circle  $x^2 + y^2 = 1$    **(b) x-axis**   (c) y-axis   (d) the lines  $x+y = 1$

32) If  $z = a + ib$  lies in quadrant then  $\frac{\bar{z}}{z}$  also lies in the III quadrant if \_\_\_\_\_

- (a)  $a > b > 0$    (b)  $a < b < 0$    **(c)  $b < a < 0$**    (d)  $b > a > 0$

33)  $\frac{1+e^{-i\theta}}{1+e^{i\theta}} =$  \_\_\_\_\_

- (a)  $\cos\theta + i\sin\theta$    **(b)  $\cos\theta - i\sin\theta$**    (c)  $\sin\theta - i\cos\theta$    (d)  $\sin\theta + i\cos\theta$

34) If  $z^n = \cos\frac{n\pi}{3} + i\sin\frac{n\pi}{3}$ , then  $z_1, z_2, \dots, z_6$  is \_\_\_\_\_

- (a) 1   **(b) -1**   (c)  $i$    (d)  $-i$

35) If  $x = \cos\theta + i\sin\theta$ , then the value of  $x^n + \frac{1}{x^n}$  is \_\_\_\_\_

- (a)  $2\cos\theta$**    (b)  $2i\sin n\theta$    (c)  $2i\sin n\theta$    (d)  $2i\cos n\theta$

36)  $\frac{(\cos\theta + i\sin\theta)^6}{(\cos\theta - i\sin\theta)^5} =$  \_\_\_\_\_

- (a)  $\cos 11\theta - i\sin 11\theta$    **(b)  $\cos 11\theta + i\sin 11\theta$**    (c)  $\cos\theta + i\sin\theta$    (d)  $\cos\frac{6\theta}{5} + i\sin\frac{6\theta}{5}$

37) The modular of  $\frac{(-1+i)(1-i)}{1+i\sqrt{3}}$  is \_\_\_\_\_

- (a)  $\sqrt{2}$    (b) 2   **(c) 1**   (d)  $\frac{1}{2}$

38) The value of  $\frac{(\cos 45^\circ + i\sin 45^\circ)^2 (\cos 30^\circ - i\sin 30^\circ)}{\cos 30^\circ + i\sin 30^\circ}$  is \_\_\_\_\_

- (a)  $\frac{1}{2} + i\frac{\sqrt{3}}{2}$    (b)  $\frac{1}{2} - i\frac{\sqrt{3}}{2}$    (c)  $-\frac{\sqrt{3}}{2} + \frac{1}{2}$    **(d)  $\frac{\sqrt{3}}{2} + \frac{1}{2}$**

39) If  $x = \cos\theta + i\sin\theta$ , then  $x^n + \frac{1}{x^n}$  is \_\_\_\_\_

- (a)  $2\cos n\theta$**    (b)  $2i\sin n\theta$    (c)  $2^n \cos\theta$    (d)  $2^n i\sin\theta$

40) If  $z_1, z_2, z_3$  are the vertices of a parallelogram, then the fourth vertex  $z_4$  opposite to  $z_2$  is \_\_\_\_\_

- (a)  $z_1 + z_2 - z_3$**    (b)  $z_1 + z_2 - z_3$    (c)  $z_1 + z_2 - z_3$    (d)  $z_1 - z_2 - z_3$

41) If  $x_r = \cos\left(\frac{\pi}{2^r}\right) + i\sin\left(\frac{\pi}{2^r}\right)$  then  $x_1, x_2, x_3, \dots, x_\infty$  is \_\_\_\_\_

- (a)  $-\infty$    (b) -2   **(c) -1**   (d) 0

42) If  $z = \frac{4+3i}{5-3i}$  then  $z^{-1} =$  \_\_\_\_\_

- (a)  $\frac{11}{25} - \frac{27}{25}i$**    (b)  $\frac{-11}{25} - \frac{27}{25}i$    (c)  $\frac{-11}{25} + \frac{27}{25}i$    (d)  $\frac{11}{25} + \frac{27}{25}i$

43) If the cube roots of unity are  $1, \omega, \omega^2$  then  $1 + \omega + \omega^2 =$  \_\_\_\_\_

- (a) 1   **(b) 0**   (c) -1   (d)  $\omega$

44) Let  $z, w$  be complex numbers such that  $\bar{z} + i\bar{w} = 0$  and  $\arg(zw) = \pi$  then  $\arg z =$  \_\_\_\_\_

- (a)  $\frac{3\pi}{4}$**    (b)  $\frac{\pi}{2}$    (c)  $\frac{\pi}{4}$    (d)  $\frac{5\pi}{4}$

45) If  $\frac{(1+i)x-2i}{3+i} + \frac{(2-3i)y+i}{3-i} = i$  then  $(x, y) =$  \_\_\_\_\_

(a) (3, 1)    **(b) (3, -1)**    (c) (-3, 1)    (d) (-3, -1)

46) Let  $z$  be complex number with modulus 2 and argument  $\frac{-2\pi}{3}$  then  $z =$  \_\_\_\_\_

(a)  $-1 + i\sqrt{3}$     (b)  $\frac{-1+i\sqrt{3}}{2}$     **(c)  $-1 - i\sqrt{3}$**     (d)  $\frac{-1-i\sqrt{3}}{2}$

47) The equation  $|z - i| + |z + i| = k$  represents an ellipse if  $k =$  \_\_\_\_\_

(a) 1    (b) 2    **(c) 4**    (d) -1

48) If  $\begin{vmatrix} 6i & -3i & 1 \\ 4 & 3i & -1 \\ 20 & 3 & i \end{vmatrix} = x + iy$  then \_\_\_\_\_

(a)  $x = 3, y = 1$     (b)  $x = 1, y = 3$     (c)  $x = 0, y = 3$     **(d)  $x = 0, y = 0$**

49) If  $z = \cos \frac{\pi}{3} - i \sin \frac{\pi}{3}$  then  $z^2 - z + 1 =$  \_\_\_\_\_

(a)  $-2i$     (b) 2    **(c) 0**    (d)  $-2$

50) All complex numbers  $z$  which satisfy the equation  $\left| \frac{z-6i}{z+6i} \right| = 1$  lie on the \_\_\_\_\_

**(a) real axis**    (b) imaginary axis    (c) circle    (d) ellipse