

QB365 Question Bank Software Study Materials

Differential Equations 50 Important 1 Marks Questions With Answers (Book Back and Creative)

12th Standard

Business Maths and Statistics

Total Marks : 50

Multiple Choice Question

50 x 1 = 50

- 1) The degree of the differential equation $\frac{d^4y}{dx^4} - \left(\frac{d^2y}{dx^2}\right)^4 + \frac{dy}{dx} = 3$ _____.
(a) 1 (b) 2 (c) 3 (d) 4
- 2) The order and degree of the differential equation $\sqrt{\frac{d^2y}{dx^2}} = \sqrt{\frac{dy}{dx} + 5}$ are respectively _____.
(a) 2 and 3 (b) 3 and 2 (c) 2 and 1 (d) 2 and 2
- 3) The order and degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^{\frac{3}{2}} - \sqrt{\left(\frac{dy}{dx}\right)} - 4 = 0$ are respectively _____.
(a) 2 and 6 (b) 3 and 6 (c) 1 and 4 (d) 2 and 4
- 4) The differential equation $\left(\frac{dx}{dy}\right)^3 + 2y^{\frac{1}{2}} = x$ is _____.
(a) of order 2 and degree 1 (b) of order 1 and degree 3 (c) of order 1 and degree 6 (d) of order 1 and degree 2
- 5) The differential equation formed by eliminating a and b from $y = ae^x + be^{-x}$ is _____.
(a) $\frac{d^2y}{dx^2} - y = 0$ (b) $\frac{d^2y}{dx^2} - \frac{dy}{dx} = 0$ (c) $\frac{d^2y}{dx^2} = 0$ (d) $\frac{d^2y}{dx^2} - x = 0$
- 6) The integrating factor of the differential equation $\frac{dx}{dy} + Px = Q$ is _____.
(a) $e^{\int P dx}$ (b) $\int P dx$ (c) $\int P dy$ (d) $e^{\int P dy}$
- 7) If $y = cx + c - c^3$ then its differential equation is _____.
(a) $y = \frac{dy}{dx} + \frac{dy}{dx} - \left(\frac{dy}{dx}\right)^3$ (b) $y = \left(\frac{dy}{dx}\right)^3 = x\frac{dy}{dx} - \frac{dy}{dx}$ (c) $\frac{dy}{dx} + y = \left(\frac{dy}{dx}\right)^3 - x\frac{dy}{dx}$ (d) $\frac{d^3y}{dx^3} = 0$
- 8) The complementary function of $(D^2 + 4)y = e^{2x}$ is _____.
(a) $(Ax + B)e^{2x}$ (b) $(Ax + B)e^{-2x}$ (c) **A cos 2x + B sin 2x** (d) $Ae^{-2x} + Be^{2x}$
- 9) The differential equation of $y = mx + c$ is _____. (m and c are arbitrary constants)
(a) $\frac{d^2y}{dx^2} = 0$ (b) $y = x\frac{dy}{dx} + c$ (c) $x dy + y dx = 0$ (d) $y dx - x dy = 0$
- 10) The particular integral of the differential equation is $\frac{d^2y}{dx^2} - 8\frac{dy}{dx} + 16y = 2e^{4x}$ _____.
(a) $\frac{x^2e^{4x}}{2!}$ (b) $\frac{e^{4x}}{2!}$ (c) **x^2e^{4x}** (d) xe^{4x}
- 11) Solution of $\frac{dy}{dx} + Px = 0$ _____.
(a) $x = ce^{py}$ (b) **$x = ce^{-py}$** (c) $x = py + c$ (d) $x = cy$
- 12) If $\sec^2 x$ is an integrating factor of the differential equation $\frac{dy}{dx} + Py = Q$ then $P =$ _____.
(a) **2 tan x** (b) $\sec x$ (c) $\cos^2 x$ (d) $\tan^2 x$
- 13) The integrating factor of $x \frac{dy}{dx} - y = x^2$ is _____.
(a) $\frac{-1}{x}$ (b) $\frac{1}{x}$ (c) $\log x$ (d) x

14) The solution of the differential equation $\frac{dy}{dx} + Py = Q$ where P and Q are the function of x is _____. (a) $y = \int Q e^{\int P dx} dx + C$ (b) $y = \int Q e^{-\int P dx} dx + C$ (c) $ye^{\int P dx} = \int Q e^{\int P dx} dx + C$ (d) $ye^{\int P dx} = \int Q e^{-\int P dx} dx + C$

15) The differential equation formed by eliminating A and B from $y = e^{-2x}(A \cos x + B \sin x)$ is _____. (a) $y_2 - 4y_1 + 5 = 0$ (b) $y_2 + 4y_1 - 5 = 0$ (c) $y_2 - 4y_1 - 5 = 0$ (d) **$y_2 + 4y_1 + 5 = 0$**

16) The particular integral of the differential equation $f(D)y = e^{ax}$ where $f(D) = (D-a)^2$ _____. (a) $\frac{x^2}{2}e^{ax}$ (b) xe^{ax} (c) $\frac{x}{2}e^{ax}$ (d) x^2e^{ax}

17) The differential equation of $x^2 + y^2 = a^2$ _____. (a) $xdy + ydx = 0$ (b) $ydx - xdy = 0$ (c) $xdx - ydy = 0$ (d) **$xdx + ydy = 0$**

18) The complementary function of $\frac{d^3y}{dx^3} - \frac{dy}{dx} = 0$ is _____. (a) **$A + Be^x$** (b) $(A + B)e^x$ (c) $(Ax + B)e^x$ (d) $Ae^x + B$

19) The P.I. of $(3D^2 + D - 14)y = 13e^{2x}$ is _____. (a) $\frac{x}{2}e^{2x}$ (b) **xe^{2x}** (c) $\frac{x^2}{2}e^{2x}$ (d) $13xe^{2x}$

20) The general solution of the differential equation $\frac{dy}{dx} = \cos x$ is _____. (a) $y = \sin x + 1$ (b) $y = \sin x - 2$ (c) $y = \cos x + c$, c is an arbitrary constant (d) **$y = \sin x + c$, c is an arbitrary constant**

21) A homogeneous differential equation of the form $\frac{dy}{dx} = f\left(\frac{y}{x}\right)$ can be solved by making substitution, _____. (a) **$y = vx$** (b) $v = y/x$ (c) $x = vy$ (d) $x = v$

22) A homogeneous differential equation of the form $\frac{dx}{dy} = f\left(\frac{y}{x}\right)$ can be solved by making substitution, _____. (a) **$x = vy$** (b) $y = vx$ (c) $y = v$ (d) $x = v$

23) The variable separable form of $\frac{dy}{dx} = \frac{y(x-y)}{x(x+y)}$ by taking $y = vx$ and $\frac{dy}{dx} = v + x\frac{dv}{dx}$ is _____. (a) $\frac{2v^2}{1+v}dv = \frac{dx}{x}$ (b) $\frac{2v^2}{1+v}dv = -\frac{dx}{x}$ (c) $\frac{2v^2}{1-v}dv = \frac{dx}{x}$ (d) **$\frac{1+v}{2v^2}dv = -\frac{dx}{x}$**

24) Which of the following is the homogeneous differential equation? (a) $(3x-5)dx = (4y-1)dy$ (b) $xy dx - (x^3+y^3)dy = 0$ (c) **$y^2dx + (x^2 - xy - y^2)dy = 0$** (d) $(x^2+y)dx = (y^2+x)dy$

25) The solution of the differential equation $\frac{dy}{dx} = \frac{y}{x} + \frac{f\left(\frac{y}{x}\right)}{f'\left(\frac{y}{x}\right)}$ is _____. (a) **$f\left(\frac{y}{x}\right) = k \cdot x$** (b) $xf\left(\frac{y}{x}\right) = k$ (c) $f\left(\frac{y}{x}\right) = ky$ (d) $yf\left(\frac{y}{x}\right) = k$

26) The differential equation of all circles with centre at the origin is _____. (a) $xdy + ydx = 0$ (b) $xdy - ydx = 0$ (c) **$xdx + ydy = 0$** (d) $xdx - ydy = 0$

27) The degree of the differential equation $\sqrt{1 + \left(\frac{dy}{dx}\right)^{\frac{1}{3}}} = \frac{d^2y}{dx^2}$ is _____. (a) 1 (b) 2 (c) 3 (d) **6**

28) The degree and order of $\frac{d^2y}{dx^2} - 6\sqrt{\frac{dy}{dx}} = 0$ are _____. (a) 2,1 (b) 1,2 (c) **2,2** (d) 1,1

29) Integrating factor of $\frac{dy}{dx} + \frac{1}{x \log x}y = \frac{2}{x^2}$ is _____. (a) e^x (b) **$\log x$** (c) $\frac{1}{x}$ (d) e^{-x}

30) The differential equation of the family of lines $y=mx$ is _____. (a) $y = mx + C$ (b) $y = mx^2 + C$ (c) $y = mx^3 + C$ (d) $y = mx^4 + C$

(a) $\frac{dy}{dx} = m$ (b) $y \, dx - x \, dy = 0$ (c) $\frac{d^2y}{dx^2} = 0$ (d) $y \, dx + x \, dy = 0$

31) The P.I. of the differential equation $f(D)y = e^{ax}$ where $f(D) = (D-a)$, $g(a) \neq 0$ is _____

(a) me^{ax} (b) $\frac{e^{ax}}{g(a)}$ (c) $g(a)e^{ax}$ (d) $\frac{xe^{ax}}{g(a)}$

32) The solution of $x \, dx + y \, dy = 0$ is _____

(a) $x^2 + y^2 = c$ (b) $\frac{x}{y} = c$ (c) $x^2 - y^2 = c$ (d) $xy = c$

33) When $y = vx$, the differential equation $x \frac{dy}{dx} = y + \sqrt{x^2 + y^2}$ reduces to _____

(a) $\frac{dv}{\sqrt{v^2-1}} = \frac{dx}{x}$ (b) $\frac{vdv}{\sqrt{v^2+1}} = \frac{dx}{x}$ (c) $\frac{dv}{\sqrt{v^2+1}} = \frac{dx}{x}$ (d) $\frac{vdv}{\sqrt{1-v^2}} = \frac{dx}{x}$

34) The solution of the equation of the type $\frac{dy}{dx} + Py = 0$ (P is a function of x) is given by _____

(a) $ye^{\int Pdx} = c$ (b) $y \int Pdx = c$ (c) $xe^{\int Pdx} = y$ (d) $y = cx$

35) The complementary function of the differential equation $(D^2 - 2D + 1)y = e^{2x}$ is _____

(a) $(Ae^x + Be^{-x})$ (b) $A + Be^x$ (c) $(Ax + B)e^x$ (d) $A + Be^{-x}$

36) The solution of $\frac{d^2y}{dx^2} - y = 0$ is _____

(a) $(A + B)e^x$ (b) $(Ax + B)e^{-x}$ (c) $Ae^x + \frac{B}{e^x}$ (d) $(A + Bx)e^{-x}$

37) A particular integral of $(3D^2 + D - 14)y = 13e^{2x}$ is _____

(a) $\frac{x^2}{2}e^{2x}$ (b) xe^{2x} (c) xe^{-2x} (d) $\frac{x}{2}e^{-2x}$

38) The particular integral of the differential equation $(D)y = e^{ax}$ wherref $(D) = (D - a)g(D)g(a) \neq 0$ is _____

(a) me^{ax} (b) $\frac{e^{ax}}{g(a)}$ (c) $g(a)e^{ax}$ (d) $\frac{xe^{ax}}{g(a)}$

39) The degree of the differential equation $\left(\frac{d^2y}{dx^2}\right)^2 - \left(\frac{dy}{dx}\right) = y^3$ is _____

(a) 1/2 (b) 2 (c) 3 (d) 4

40) The degree of the differential equation $\left[5 + \left(\frac{dy}{dx}\right)^2\right]^{5/3} = x^5 \left(\frac{d^2y}{dx^2}\right)$ is _____

(a) 4 (b) 3 (c) 5 (d) 10

41) The equation of the curve whose slope is given by $\frac{dy}{dx} = \frac{2y}{x}$, $x > 0$, $y > 0$ and which passes through the point (1, 1) is _____

(a) $x^2 = y$ (b) $y^2 = x$ (c) $x^2 = 2y$ (d) $y^2 = 2x$

42) The solution of the differential equation $\frac{dy}{dx} - \frac{y(x+1)}{x} = 0$ is given by _____

(a) $y = xe^{x+c}$ (b) $x = ye^x$ (c) $y = x + c$ (d) $xy = e^x + c$

43) The solution of the differential equation $x \frac{dy}{dx} = y + x \tan \frac{y}{x}$ is _____

(a) $\sin \frac{x}{y} = x + c$ (b) $\sin \frac{y}{x} = cx$ (c) $\sin \frac{x}{y} = cy$ (d) $\sin \frac{y}{x} = cy$

44) The differential equation satisfied by $ax^2 + bx^2 = 1$ is _____

(a) $xyy_2 + y_1^2 + yy_1 = 0$ (b) $xyy_2 + xy_1^2 - yy_1 = 0$ (c) $xyy_2 - xy_1^2 + yy_1 = 0$ (d) none of these

45) The solution of the differential equation $(x^2 + 1) \frac{dy}{dx} + (y^2 + 1) = 0$ is _____

(a) $y = 2 + x^2$ (b) $y = \frac{1+x}{1-x}$ (c) $y = x(x-1)$ (d) $y = \frac{1-x}{1+x}$

46) The differential equation $x \frac{dy}{dx} - y = x^2$ has the general solution _____

(a) $y - x^3 = 2cx$ (b) $2y - x^3 = cx$ (c) $2y + x^2 = 2cx$ (d) $y + x^2 = 2cx$

47) What is the integrating factor of $\frac{dy}{dx} + y \sec x = \tan x$?

- (a) **sec x + tan x** (b) log (sec x + tan x) (c) $e^{\sec x}$ (d) sec x

48) The order of the differential equation $2x^2 \frac{d^2y}{dx^2} - 3\frac{dy}{dx} + y = 0$ is _____

- (a) **2** (b) 1 (c) 0 (d) not defined

49) Which of the following differential equation has $y = c_1 e^x + c_2 e^{-x}$ as the general solution?

- (a) $\frac{d^2y}{dx^2} + y = 0$ (b) **$\frac{d^2y}{dx^2} - y = 0$** (c) $\frac{d^2y}{dx^2} + 1 = 0$ (d) $\frac{d^2y}{dx^2} - 1 = 0$

50) In interpolation the independent variable y is called the _____

- (a) **entry** (b) argument (c) modulus (d) amplitude