

QB365 Question Bank Software Study Materials

Coordinate Geometry Important 2 Marks Questions With Answers (Book Back and Creative)

9th Standard

Maths

Total Marks : 60

2 Marks

30 x 2 = 60

- 1) In which quadrant does the following points lie?(2, 5)

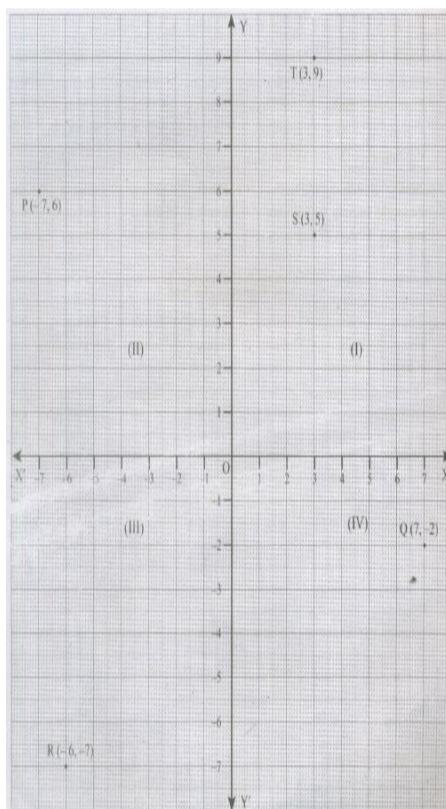
Answer : The x-coordinate is positive and y – coordinate is positive. So Point (2,5) lies in the I quadrant

- 2) In which quadrant does the following points lie?(-7, 3)

Answer : The x-coordinate is negative and y – coordinate is positive. So, Point(-7,3) lies in the II quadrant

- 3) Plot the following points in the coordinate system and identify the quadrants

P(-7, 6), Q(7, -2), R(-6, -7), S(3, 5) and T(3, 9)

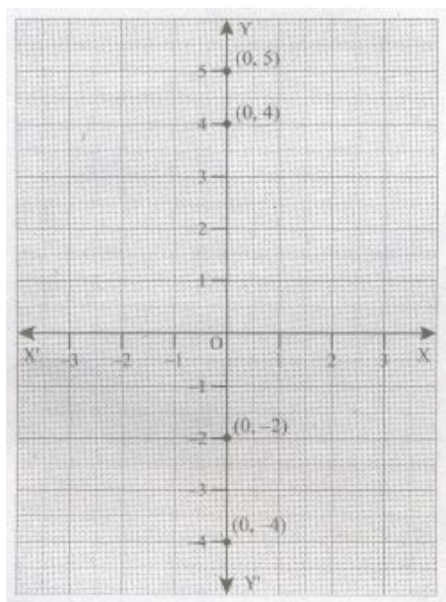


Answer :

- (i) P (-7, 6) lies in the II quadrant because the x-coordinate is negative and y-coordinate is positive
- (ii) Q (7, -2) lies in the IV quadrant because the x-coordinate is positive and y-coordinate is negative
- (iii) R (-6, -7) lies in the III quadrant because the x-coordinate is negative and y-coordinate is negative
- (iv) S (3, 5) lies in the I quadrant because the x-coordinate is positive and y-coordinate is also positive
- (v) T (3, 9) lies in the I quadrant because the x-coordinate is positive and y-coordinate is also positive

- 4) Plot the following points in the coordinate plane and join them. What is your conclusion about the resulting figure?

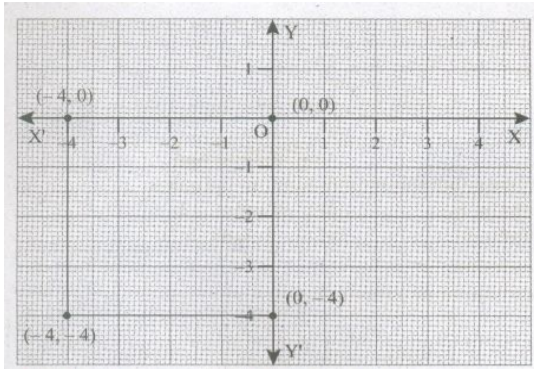
(0, -4) (0, -2) (0, 4) (0, 5)



Answer :

The line is on the y - axis

- 5) Plot the following points in the coordinate plane. Join them in order. What type of geometrical shape is formed?
 (0, 0) (-4, 0) (-4, -4) (0, -4)



Answer :

The geometrical shape of the figure is square

- 6) Find the distance between the following pairs of points. (1, 2) and (4, 3)

Answer : Distance between the points (1, 2) and (4, 3)

$$\begin{aligned}
 &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
 &= \sqrt{(4 - 1)^2 + (3 - 2)^2} = \sqrt{3^2 + 1^2} \\
 &= \sqrt{9 + 1} = \sqrt{10} = \text{units}
 \end{aligned}$$

- 7) Find the distance between the following pairs of points. (3,4) and (-7, 2)

Answer : Distance between the points (3,4) and (-7, 2)

$$\begin{array}{r}
 2 \overline{)104} \\
 \underline{2 52} \\
 2 \underline{26} \\
 13
 \end{array}$$

$$\begin{aligned}
 &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
 &= \sqrt{(-7 - 3)^2 + (2 - 4)^2} = \sqrt{(-10)^2 + (-2)^2} \\
 &= \sqrt{100 + 4} = \sqrt{104} = \sqrt{2^2 \times 2 \times 13} \\
 &= 2\sqrt{26} \text{ units}
 \end{aligned}$$

- 8) Find the distance between the following pairs of points.(a, b) and (c, b)

Answer : Distance between the two points (a, b) and (c, b)

$$\begin{aligned}
 &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
 &= \sqrt{(c - a)^2 + (b - b)^2} = \sqrt{(c - a)^2} \\
 &= c - a \text{ units}
 \end{aligned}$$

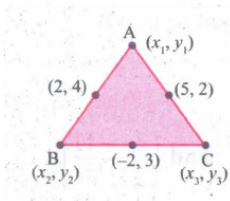
- 9) Find the distance between the following pairs of points. (3,- 9) and (-2, 3)

Answer : Distance between the two points (3,- 9) and (-2, 3)

$$\begin{aligned}
 &= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \\
 &= \sqrt{(-2 - 3)^2 + (3 + 9)^2} = \sqrt{(-5)^2 + (12)^2} \\
 &= \sqrt{25 + 144} = \sqrt{169} = 13 \text{ units}
 \end{aligned}$$

- 10) The mid-point of the sides of a triangle are (2, 4), (-2, 3) and (5, 2). Find the coordinates of the vertices of the triangle.

Answer :



Mid point

$$M(x, y) = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

$$\text{Mid point AB}(2, 4) = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

$$\frac{x_1+x_2}{2} = 2 \Rightarrow x_1 + x_2 = 4 \quad \dots (1)$$

$$\frac{y_1+y_2}{2} = 4 \Rightarrow y_1 + y_2 \quad \dots (2)$$

$$\text{Mid point of BC } (-2, 3) = \left(\frac{x_2+x_3}{2}, \frac{y_2+y_3}{2} \right)$$

$$\left(\frac{x_2+x_3}{2} \right) = -2 \Rightarrow x_2 + x_3 = -4 \quad \dots (3)$$

$$\left(\frac{y_2+y_3}{2} \right) = 3 \Rightarrow y_2 + y_3 = 6 \quad \dots (4)$$

$$\text{Mid point of AC } (5, 2) = \left(\frac{x_1+x_3}{2}, \frac{y_1+y_3}{2} \right)$$

$$\left(\frac{x_1+x_3}{2} \right) = 5 \Rightarrow x_1 + x_3 = 10 \quad \dots (5)$$

$$\frac{y_1+y_3}{2} = 2 \Rightarrow y_1 + y_3 = 4 \quad \dots (6)$$

$$(1) - (3) \Rightarrow x_1 + x_2 = 4$$

$$x_2 + x_3 = -4$$

$$\hline x_1 - x_3 = 8$$

$$(5) \Rightarrow x_1 + x_3 = 10$$

$$x_1 - x_3 = 8$$

$$\hline 2x_1 = 18$$

$$x_1 = 9$$

Substitute $x_1 = 9$ in (5)

$$9 + x_3 = 10$$

$$x_3 = 1$$

Substitute $x_1 = 9$ in (3)

$$x_2 + 1 = -4 \Rightarrow x_2 = -5$$

$$\text{similarly } (2) - (4) \Rightarrow y_1 + y_2 = 8$$

$$(6) \Rightarrow y_1 + y_3 = 4$$

$$y_2 + y_3 = 6$$

$$\hline y_1 - y_3 = 2$$

$$\hline 2y_1 = 6$$

$$y_1 = 3$$

substitute $y_1 = 3$ in (6)

$$3 + y_3 = 4$$

$$y_3 = 1$$

substitute $y_3 = 1$ in (4)

$$1 + y_2 = 6$$

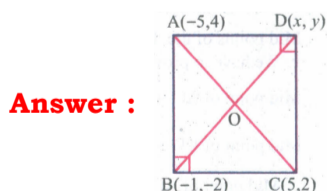
$$y_2 = 5$$

∴ The vertices of the triangle $A(x_1, y_1) = (9, 3)$

$$B(x_2, y_2) = (-5, 5)$$

$$C(x_3, y_3) = (1, 1)$$

- 11) The points $A(-5, 4)$, $B(-1, -2)$ and $C(5, 2)$ are the vertices of an isosceles rightangled triangle where the right angle is at B. Find the coordinates of D so that ABCD is a square.



In squares the diagonals are equal and bisect each other

∴ Mid point of BD = Mid point of AC

$$\left(\frac{-1+x}{2}, \frac{-2+y}{2} \right) = \left(\frac{-5+5}{2}, \frac{4+2}{2} \right)$$

$$\frac{-1+x}{2} = \frac{0}{2} \quad \frac{-2+y}{2} = \frac{6}{2}$$

$$-1 + x = -2 + y = 6$$

$$x = 1 \quad y = 8$$

∴ The vertex $D(x, y) = (1, 8)$

- 12) The points $A(-3, 6)$, $B(0, 7)$ and $C(1, 9)$ are the mid-points of the sides DE, EF and FD of a triangle DEF. Show that the quadrilateral ABCD is a parallelogram.

Answer : In a parallelogram diagonals bisect each other and diagonals are not equal.

$$\text{Mid point of DE} = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

$$(-3, 6) = \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2} \right)$$

$$\frac{x_1+x_2}{2} = -3 \quad \frac{y_1+y_2}{2} = 6$$

$$x_1 + x_2 = -6 \dots\dots(1)$$

$$y_1 + y_2 = 12 \dots\dots(2)$$

$$\text{Mid point of EF} = \left(\frac{x_2+x_3}{2}, \frac{y_2+y_3}{2} \right)$$

$$(0, 7) = \left(\frac{x_2+x_3}{2}, \frac{y_2+y_3}{2} \right)$$

$$\frac{x_2+x_3}{2} = 0 \quad \frac{y_2+y_3}{2} = 7$$

$$x_2+x_3 = 0 \dots\dots(3)$$

$$\text{Mid point of FD} = \left(\frac{x_3+x_1}{2}, \frac{y_3+y_1}{2} \right) = (-3, -2)$$

$$x_3 + x_1 = -6 \dots\dots(5)$$

$$y_3 + y_1 = -4 \dots\dots(6)$$

$$(1)-(3) \Rightarrow \begin{matrix} x_1 + x_2 = -6 \\ x_3 + x_2 = 0 \end{matrix} \quad (2)-(4) \Rightarrow \begin{matrix} y_1 + y_2 = 12 \\ y_3 + y_2 = 14 \end{matrix}$$

$$(5) \Rightarrow \begin{matrix} x_1 - x_3 = -6 \\ x_1 + x_3 = -6 \end{matrix} \quad (6) \Rightarrow \begin{matrix} y_1 - y_3 = -2 \\ y_1 + y_3 = -4 \end{matrix}$$

$$\begin{matrix} 2x_1 = -12 \\ x_1 = -6 \end{matrix} \quad \begin{matrix} 2y_1 = -6 \\ y_1 = -3 \end{matrix}$$

$$\therefore D(x_1, y_1) = (-6, -3)$$

Mid points of the diagonals are equal in parallelogram

\therefore We have to prove this

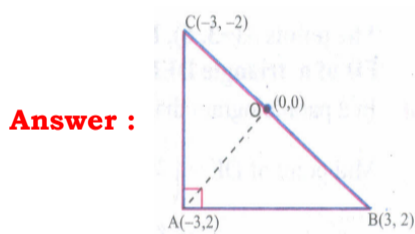
$$\text{Mid point of AC} = \left(\frac{(-3)+(-3)}{2}, \frac{6+(-2)}{2} \right) = \left(\frac{-6}{2}, \frac{4}{2} \right) = (-3, 2)$$

$$\text{Mid Point of BD} = \left(\frac{-6+0}{2}, \frac{-3+7}{2} \right) = \left(\frac{-6}{2}, \frac{4}{2} \right) = (-3, 2)$$

\therefore Mid point of AC = Mid point of BD

\therefore ABCD is a parallelogram

- 13) A(-3,2), B(3,2) and C(-3,-2) are the vertices of the right triangle, right angled at A. Show that the mid-point of the hypotenuse is equidistant from the vertices.



Answer :

$$= \left(\frac{2+(-3)}{2}, \frac{2+(-2)}{2} \right)$$

$$= \left(\frac{0}{2}, \frac{0}{2} \right) = (0, 0)$$

Distance between two points

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\bar{OA} = \sqrt{(-3 - 0)^2 + (2 - 0)^2}$$

$$= \sqrt{(-3)^2 + 2^2} = \sqrt{9 + 4} = \sqrt{13}$$

$$\bar{OB} = \sqrt{(-3 - 0)^2 + (2 - 0)^2} = \sqrt{9 + 4} = \sqrt{13}$$

$$\bar{OC} = \sqrt{(-3 - 0)^2 + (-2 - 0)^2} = \sqrt{9 + 4} = \sqrt{13}$$

$\therefore \bar{OA} = \bar{OB} = \bar{OC}$ Hence Proved

- 14) Find the coordinates of the point which divides the line segment joining the points A(4,-3) and B(9,7) in the ratio 3:2.

Answer : $x_1 y_1 \quad x_2 y_2 \quad m : n$

A (4, -3), B (9, 7), 3 : 2

$$\text{By section formula } P \left(\frac{mx_2+nx_1}{m+n}, \frac{my_2+ny_1}{m+n} \right) = P(x, y)$$

$$\frac{3}{A(4, -3)} \quad \frac{2}{P(x, y)} \quad \frac{2}{B(9, 7)}$$

$$P(x, y) = \left(\frac{3(9)+2(4)}{3+2}, \frac{3(7)+2(-3)}{3+2} \right)$$

$$= \left(\frac{27+8}{5}, \frac{21-6}{5} \right) = \left(\frac{35}{5}, \frac{15}{5} \right) = (7, 3)$$

- 15) In what ratio does the point P(2, -5) divide the line segment joining A(-3, 5) and B(4, -9) .

Answer : $x_1 y_1 \quad x_2 y_2$

A(-3, 5) B(4, -9) P(2, -5)

$$= P(x, y) \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$$

$$P(2, -5) = \left(\frac{m \times 4 + n(-5)}{m+n}, \frac{m \times (-9) + n(5)}{m+n} \right)$$

$$\left(\frac{4m-3n}{m+n} \right) = 2$$

$$4m - 3n = 2m + 2n$$

$$4m - 2m = 2n + 3n$$

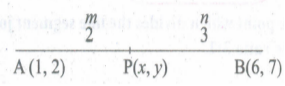
$$2m = 5n$$

$$\frac{m}{n} = \frac{5}{2}$$

\therefore The ratio $m : n = 5 : 2$

- 16) Find the coordinates of a point P on the line segment joining A(1, 2) and B(6, 7) in such a way that $AP = \frac{2}{5}AB$

Answer :



$x_1 y_1 \quad x_2 y_2$

A(1, 2) B(6, 7)

$$= P(x, y) \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$$

$$= \left(\frac{2 \times 6 + 3 \times 1}{2+3}, \frac{2 \times 7 + 3 \times 2}{2+3} \right)$$

$$= \left(\frac{12-3}{5}, \frac{14+6}{5} \right) = \left(\frac{15}{5}, \frac{20}{5} \right) = (3, 4)$$

- 17) The line segment joining A(6, 3) and B(-1, -4) is doubled in length by adding half of AB to each end. Find the coordinates of the new end points.

Answer : $D(x_4, y_4)$ $A(6, 3)$ $M\left(\frac{5}{2}, \frac{-1}{2}\right)$ $B(-1, -4)$ $C(x_3, y_3)$

$$\bar{AB} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(-1 - 6)^2 + (-4 - 3)^2}$$

$$= \sqrt{(-7)^2 + (-7)^2} = \sqrt{49 + 49} = \sqrt{(49)2}$$

$$\frac{1}{2}AB = \frac{7\sqrt{2}}{2} = \frac{7\sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{7}{\sqrt{2}}$$

$$AB = \left(\frac{6+(-1)}{2}, \frac{3+(-4)}{2}\right) = \left(\frac{5}{2}, \frac{-1}{2}\right)$$

$$\text{Mid point of } AB = \left(\frac{6+(-1)}{2}, \frac{3+(-4)}{2}\right) = \left(\frac{5}{2}, \frac{-1}{2}\right)$$

Since C is at the distance $\frac{1}{2}$ AB from B

Midpoint of MC = B

$$\left(\frac{\frac{5}{2} + x_3}{2}, \frac{\frac{-1}{2} + y_3}{2}\right) = (-1, -4)$$

$$\left(\frac{\frac{5}{2} + x_3}{2}\right) = -1$$

$$\frac{5}{2} + x_3 = -2$$

$$x_3 = -2 - \frac{5}{2}$$

$$= \frac{-4-5}{2}$$

$$= \frac{-9}{2}$$

$$\therefore C(x_3, y_3) = \left(\frac{-9}{2}, \frac{-15}{2}\right)$$

$$\left(\frac{\frac{-1}{2} + y_3}{2}\right) = -4$$

$$|-\frac{1}{2} + y_3 = -8$$

$$y_3 = -8 + \frac{1}{2}$$

$$= \frac{-16+1}{2}$$

$$= \frac{-15}{2}$$

Similarly by Mid point of DM = A(6, 3)

$$\left(\frac{x_4 + \frac{5}{2}}{2}, \frac{y_4 + \left(\frac{-1}{2}\right)}{2}\right) = (6, 3)$$

$$\frac{x_4 + \frac{5}{2}}{2} = 6$$

$$x_4 + \frac{5}{2} = 12$$

$$x_4 = 12 - \frac{5}{2} = \frac{24-5}{2} = \frac{19}{2}$$

$$\frac{y_4 + \left(\frac{-1}{2}\right)}{2} = 3$$

$$y_4 + \left(\frac{-1}{2}\right) = 6$$

$$y_4 = 6 + \frac{1}{2} = \frac{12+102}{2} = \frac{13}{2}$$

$$\therefore \text{The other end } D(x_4, y_4) = \left(\frac{19}{2}, \frac{13}{2}\right)$$

18) Find the centroid of the triangle whose vertices are

(i) (2, -4), (-3, -7) and (7, 2)

(ii) (-5, -5), (1, -4) and (-4, -2)

Answer : $x_1 y_1 x_2 y_2 x_3 y_3$

(2, -4) (-3, -7) (7, 2)

$$(i) \text{ Centroid } G(x, y) = \left(\frac{x_1 + x_2 + x_3}{3}, \frac{y_1 + y_2 + y_3}{3}\right)$$

$$= \left(\frac{(2)+(-3)+7}{3}, \frac{(-4)+(-7)+(2)}{3}\right)$$

$$= \left(\frac{6}{3}, \frac{-9}{3}\right) = (2, -3)$$

(ii) $x_1 y_1 x_2 y_2 x_3 y_3$

(2, -4) (1, -4) (-4, -2)

$$\text{Centroid } G(x, y) = \left(\frac{(-5)+1+(-4)}{3}, \frac{(-5)+(-4)+(-2)}{3}\right)$$

$$= \left(\frac{-8}{3}, \frac{-11}{3}\right)$$

19) If the centroid of a triangle is at (4, -2) and two of its vertices are (3, -2) and (5, 2) then find the third vertex of the triangle.

Answer : Centroid G (x,y) = (4, -2)

two vertices $(x_1, y_1) = (3, -2)$

$(x_2, y_2) = (5, 2), (x_3, y_3) = ?$

$$(4, -2) = \left(\frac{3+5+x_3}{3}, \frac{-2+2+y_3}{3} \right)$$

$$(4, -2) = \left(\frac{8+x_3}{3}, \frac{y_3}{3} \right)$$

$$\frac{8+x_3}{3} = 4 \quad \frac{y_3}{3} = -2$$

$$8 + x_3 = 12 \quad y_3 = -6$$

$$x_3 = 4$$

\therefore The third vertex $(x_3, y_3) = (4, -6)$

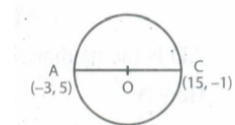
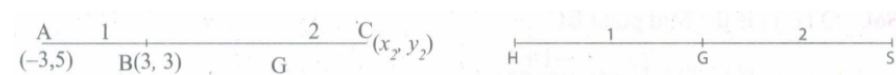
- 20) Orthocentre and centroid of a triangle are A(-3, 5) and B(3,3) respectively. If C is the circumcentre and AC is the diameter of this circle, then find the radius of the circle.

Answer : H = A (-3, 5)

G = B (3, 3)

S = Circumcentre (C)

G divides HS in the ratio 2 : 1



$$m : n = 1 : 2$$

A(x₂, y₁) = (-3, 5)

C(x₂, y₂) = (x₂, y₂)

P (x, y) = (3, 3)

$$\therefore P(x, y) = \left(\frac{mx_2+nx_1}{m+n}, \frac{my_2+ny_1}{m+n} \right)$$

$$(3, 3) = \left(\frac{1x_2+2(-3)}{2+1}, \frac{1(y_2)+2(5)}{2+1} \right)$$

$$(3, 3) = \left(\frac{x_2-6}{3}, \frac{y_2+10}{3} \right)$$

$$\frac{x_2-6}{3} = 3$$

$$x_2 - 6 = 9$$

$$x_2 = 9 + 6$$

$$x = 15$$

$$\frac{y_2+10}{3} = 3$$

$$y_2+10 = 9$$

$$y_2 = 9-10$$

$$y_2 = -1$$

$$\overline{AC} = \sqrt{(5 - (-3))^2 + (-1 - 5)^2}$$

$$= \sqrt{8^2 + (-6)^2} = \sqrt{324 + 36}$$

$$= \sqrt{360} = \sqrt{36 \times 10} = 6\sqrt{10}$$

$$\text{radius} = \frac{1}{2}AC$$

$$= \frac{1}{2} \times 6\sqrt{10} = 3\sqrt{10} \text{ units.}$$

$$\text{Radius} = \frac{3}{2}\sqrt{10} \text{ or } 3\sqrt{\frac{10}{4}}$$

$$= 3\sqrt{\frac{5}{2}} \text{ units}$$

\therefore AC is a diameter of circle

- 21) Find the coordinates of the point which divides the line segment joining A(-5,11) and B(4,-7) in the ratio 7:2.

Answer : $\frac{7}{A(-5, 11) \quad P(x, y) \quad B(4, -7)}$

$x_1 y_1$

Here $(-5, 11)$

$x_2 y_2$

$(4, -7)$

$m n$

$7 : 2$

$$\begin{aligned}
 &= P(x, y) \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right) \\
 &= \left(\frac{7 \times 4 + 2 \times (-5)}{7+2}, \frac{7 \times (-7) + 2 \times 11}{7+2} \right) \\
 &= \left(\frac{28-10}{9}, \frac{-49+22}{9} \right) \\
 &= \left(\frac{18}{9}, \frac{-27}{9} \right) = (2, -3)
 \end{aligned}$$

- 22) A car travels at a uniform speed. At 2 pm it is at a distance of 180 km and at 6pm it is at 360 km. Using section formula, find at what distance it will reach 12 midnight.

Answer : $\frac{2pm \quad m \quad 6pm \quad n \quad 12 \text{ midnight}}{A \quad B}$
 $\frac{180 \text{ km} \quad 360 \text{ km} \quad (12, \alpha)}{(2, 180) \quad (6, 360)}$

Dividing point $(x, y) = \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$

$$(6, 360) = \left(\frac{m \times 12 + n \times 2}{m+n}, \frac{m \alpha + n \times 180}{m+n} \right)$$

$$\Rightarrow \frac{12m + 2n}{m+n} = 6$$

$$12m + 2n = 6m + 6n$$

$$12m - 6m = 6n - 2n$$

$$6m = 4n$$

$$\frac{m}{n} = \frac{4}{6} = \frac{2}{3}$$

$$m = \frac{2}{3}n \quad \dots(1)$$

$$\Rightarrow \frac{m\alpha + 180n}{m+n} = 360 \quad \dots(2)$$

$$\Rightarrow \frac{\frac{2}{3}n\alpha + 180n}{\frac{2}{3}n + n} = 360$$

$$\Rightarrow \frac{\left(\frac{2}{3}\alpha + 180\right) \cancel{n}}{\left(\frac{2}{3} + 1\right) \cancel{n}} = 360$$

$$\Rightarrow \frac{\frac{2}{3}\alpha + 180}{\frac{2}{3} + 1} = 360$$

$$\Rightarrow \frac{2}{3}\alpha = 240 + 360 - 180$$

$$\frac{2}{3}\alpha = 600 - 180$$

$$\frac{2}{3}\alpha = 420$$

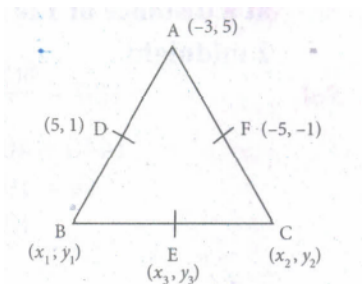
$$\alpha = 420 \times \frac{3}{2} = 630$$

$$\alpha = 630$$

\therefore The car will reach 630km at 12midnight

- 23) A, B and C are vertices of ΔABC . D, E and F are mid points of sides AB, BC and AC respectively. If the coordinates of A, D and F are $(-3, 5)$, $(5, 1)$ and $(-5, -1)$ respectively. Find the coordinates of B, C and E.

Answer :



$$(5, 1) = \left(\frac{x_1 - 3}{2}, \frac{y_1 + 5}{2} \right)$$

$$\frac{x_1 - 3}{2} = 5, \quad \frac{y_1 + 5}{2} = 2$$

$$x_1 - 3 = 10, \quad y_1 + 5 = 2$$

$$x_1 = 13, \quad y_1 = -3$$

$$B(13, -3)$$

$$(-5, -1) = \left(\frac{-3 + x_2}{2}, \frac{5 + y_2}{2} \right)$$

$$\frac{-3 + x_2}{2} = -5,$$

$$-3 + x_2 = -10$$

$$x_2 = -7,$$

$$C(-7, -7)$$

$$\frac{5 + y_2}{2} = -1$$

$$5 + y_2 = -2$$

$$y_2 = -7$$

$$(x_3, y_3) = \left(\frac{13 + (-7)}{2}, \frac{-3 + (-7)}{2} \right) = (3, -5)$$

- 24) If A (10, 11) and B (2, 3) are the coordinates of end points of diameter of circle. Then find the centre of the circle.

Answer : Centre of the circle = $\left(\frac{10+2}{2}, \frac{11+3}{2} \right) = (6, 7)$

- 25) Using section formula, show that the points A (7, -5), B (9, -3) and C (13, 1), are collinear.

Answer : $(9, -3) = \left(\frac{m(12+n(7))}{m+n}, \frac{m(1)+n(-5)}{m+n} \right)$

$$\frac{13m+37n}{m+n} = 9$$

$$13m + 7n = 9m + 9n$$

$$4m = 2n$$

$$\frac{m}{n} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{m-5n}{m+n} = -3$$

$$m - 5n = -3m - 3n$$

$$m + 3m = 5n - 3n$$

$$4m = 2n$$

$$\frac{m}{n} = \frac{2}{4} = \frac{1}{2}$$

- 26) A car travels, at an uniform speed. At 2 pm it is at a distance of 5 km at 6 pm it is at a distance of 120 km. Using section formula, find at what distance it will reach 2 midnight.

Answer : $120 = \frac{8(50)+4(y)}{12}$

$$1440 = 400 + 4y$$

$$4y = 1040$$

$$y = \frac{1040}{4} = 260 \text{ km}$$

- 27) Find the centroid of the triangle whose vertices are (2, -5), (5, 11) and (9, 9)

Answer : $G \left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3} \right) = \left(\frac{2+5+9}{3}, \frac{-5+11+9}{9} \right) = \left(\frac{16}{3}, 5 \right)$

- 28) Find the distance between the points (-4, 0) and (3, 0).

Answer : The points (-4, 0), (3, 0) lie on the x axis

$$\text{Hence } d = |x_1 - x_2| = |3 - (-4)| = |3 + 4| = 7$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(3 + 4)^2 + 0^2} = \sqrt{49} = 7$$

- 29) The radius of a circle with centre at the origin is 10 units. Write the coordinates of the points where the circle intersects the axes. Find the distance between any two such points.

Answer : Given C(0, 0), r = 10 units

It is clearly that P (0, 0). Q (0, 10)

$$\begin{aligned}\therefore d &= \sqrt{(0 - 10)^2 + (10 - 0)^2} \\ &= \sqrt{100 + 100} = \sqrt{200} = 10\sqrt{2} \text{ units}\end{aligned}$$

30) Find the centroid of the triangle whose vertices are A (4, -6), B (3, -2), C (5, 2).

Answer : The centroid G (x, y) of a triangle whose vertices are

$(x_1, y_1), (x_2, y_2), (x_3, y_3)$ is given by

$$G(x, y) = G\left(\frac{x_1+x_2+x_3}{3}, \frac{y_1+y_2+y_3}{3}\right)$$

$$(x_1, y_1) = (4, -6); (x_2, y_2) = (3, -2); (x_3, y_3) = (5, 2)$$

The centroid of the triangle whose vertices are

$$(4, -6), (3, -2), (5, 2)$$

$$G(x, y) = G\left(\frac{4+3+5}{3}, \frac{-6-2+2}{3}\right)$$

$$= G(4, -2)$$